

# What Should I Be When I Grow Up? Occupations and Unemployment over the Life Cycle\*

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## Abstract

Why is unemployment higher for younger individuals? We address this question in a frictional model of the labor market that features learning about occupational fit. In order to learn the occupation in which they are most productive, workers sample occupations over their careers. Because young workers are more likely to be in matches that represent a poor occupational fit, they spend more time in transition between occupations. Through this mechanism, our model can replicate the observed age differences in unemployment which, as in the data, are due to differences in job separation rates.

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# 1 Introduction

Labor market outcomes differ greatly for individuals of different ages. Unemployment rates are much higher for the young than for all others. For example, in the U.S., the unemployment rate for individuals aged 20–24 years old is approximately 2.5 times that of prime-aged individuals aged 45–54 years old; the unemployment rate of 25–34 year olds is about 50% greater than that of 45–54 year olds.<sup>1</sup>

In our view, explaining this fact is interesting in its own right, given that the age differences are so stark. Moreover, we believe that developing such an explanation is important for our understanding of aggregate labor market dynamics. For example, the results of [Shimer \(1998\)](#) indicate that compositional change in the labor force due to the baby boom generated a substantial fraction of the rise and fall in U.S. unemployment from the 1960s through to the end of the century.

In [Section 2](#), we detail the declining age profile for unemployment observed in the postwar U.S. data. In particular, we discuss the role of age differences in the *job finding rate* (the rate at which individuals transition from unemployment to employment) and the *separation rate* (the transition rate from employment to unemployment) in shaping the age profile of unemployment. Job separation rates decline monotonically with age, generating a declining profile of unemployment. Job finding rates exhibit much less age variation, and in fact, decline with age. On its own, the declining pattern of job finding rates would counterfactually imply an increasing age profile of unemployment. Hence, unemployment differences are accounted for solely by age differences in job separation.

Given this fact, [Sections 3](#) and [4](#) present and characterize a model that focuses on differences in the separation rate. Our model is a life-cycle version of the search-and-matching framework of [Diamond \(1982\)](#), [Mortensen \(1982\)](#) and [Pissarides \(1985\)](#) (DMP, hereafter). The key life-cycle feature that we introduce is learning on the worker’s part about her best occupational fit. Specifically, young workers enter the labor market not knowing the occupation that they are most productive in. We call this occupation the worker’s “true calling.”

In order to learn her true calling, a worker must sample occupational matches over her career. Upon entering the workforce, a worker searches for her first job in an occupation. Upon meeting a vacancy, a match is established. Over time, the worker and firm learn whether the current occupation is the worker’s true calling. If it is not, the worker-firm pair

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<sup>1</sup>See also [Shimer \(1998\)](#) and the references therein.

can either maintain the match or choose to separate. Upon separation, the worker seeks employment in a new occupation, having ruled out the previous occupation as being her true calling. As the worker samples more occupations and accumulates knowledge about her occupational fit, the probability of finding her true calling rises.

Match formation, learning, and separation are stochastic in our framework. As such, *ex ante* identical individuals experience different histories over time, as they move in and out of unemployment, and learn, more or less quickly, about their true calling. Despite this heterogeneity, workers can be summarized simply by their *type*: lower type workers have little information about their true calling, while higher types are closer to discovering it. Hence, the model generates an endogenous mapping between type and age.

This allows us to address the differences in unemployment between young and old workers. Since lower type matches are more likely to turn out to be bad matches, they are more likely to endogenously separate. Thus, lower type workers—who tend to be young—experience higher unemployment rates, as they are more likely to be in transition between occupations. As documented by [Kambourov and Manovskii \(2008\)](#) and shown in the next section, this emphasis on the age profile of occupational mobility is highly supported by U.S. longitudinal data.

In [Section 5](#), we calibrate our model and study its quantitative implications. Our model does a very good job of matching the observed age profile of unemployment. This is because our model nearly replicates the declining age profile of separation rates observed in the data. In addition, our model does a good job of matching the age profile of occupational mobility.

In [Section 6](#), we consider two applications of our model. We first demonstrate that accounting for labor force aging enables the model to rationalize a significant portion of the fall in aggregate unemployment observed in the U.S. since the mid-1970s, as emphasized in the empirical results of [Shimer \(1998\)](#). We then illustrate how a simple extension allows the model to rationalize the heterogeneous responses of earnings and wages to match separations, as documented in the empirical literature on job displacements. Hence, taken together with the results in [Section 5](#), we find that the “learning about occupational fit” mechanism is important for understanding a number of key features regarding life-cycle and aggregate labor market dynamics.

Our paper is not the first to emphasize the role of occupational fit in a labor market search framework. Our framework is related to the one-sided search problem studied by [Neal \(1999\)](#), in which employment relationships have two components: “career” quality and match quality. One interpretation of our model is that individuals are searching for a career

by sampling occupations. As such, our model is consistent with [Neal \(1999\)](#)'s empirical findings that career change falls with labor market experience. However, since that model abstracts from unemployment as a labor market state, it does not address the age profile of unemployment rates, our subject of principal interest. More recently, [Papageorgiou \(2014\)](#) also studies learning about unobserved occupational ability in a search framework. However, because the phenomena of interest are different, a number of model features differ. [Papageorgiou \(2014\)](#) finds that a calibrated version of his model does well in accounting for life-cycle wage dynamics, residual wage inequality, and inter-occupational flows. By contrast, our paper studies the role of learning about occupational fit in accounting for the life-cycle profile of unemployment and separation rates, and aggregate unemployment dynamics. Both papers do well in accounting for the life-cycle pattern of occupational mobility.

Finally, ours is not the first frictional labor market model to address age differences in unemployment. [Jovanovic \(1979\)](#) represents a seminal contribution to the literature on endogenous job separations. In that model, a worker's separation rate falls with tenure in a match. This arises because productivity in a worker-firm match is stochastic and observed imprecisely; longer tenured matches are those in which the worker and firm have learned that idiosyncratic match quality is high. [Menzio et al. \(2015\)](#) illustrate how this mechanism generates a declining age profile of separation in a life-cycle model: since young workers have drawn fewer matches, they are more likely to be in ones with lower idiosyncratic productivity, and hence, more likely to separate.<sup>2</sup>

The key distinction in our model is what is being learned in a match. In the [Jovanovic \(1979\)](#) framework, agents learn about the match quality between worker and firm, or *firm-specific* human capital. Since this is independent across matches, separation from any one match imparts no information about a worker's productivity and separation rate in future matches. In our model, agents learn about match quality between worker and occupation. This is a form of *general* human capital—knowledge of one's true calling—that worker's carry forward into the future. Separation from a match is due to the accumulation of this human capital, and generates a lower probability of separation and higher expected productivity in future matches. In contrast to the [Jovanovic \(1979\)](#) and [Menzio et al. \(2015\)](#) mechanism where young workers are more likely to be in matches with lower firm-specific

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<sup>2</sup>Finally, see also [Esteban-Pretel and Fujimoto \(2014\)](#). In their model, older workers are assumed to be better able to observe idiosyncratic match productivity, and hence, reject poor matches before they are formed. In this way, their model generates a declining age profile of separation by construction. See also [Gorry \(2012\)](#) for a one-sided search model in which labor market experience provides a worker with better information about future match quality.

Table 1: Average Unemployment Rates by Age Group

	20–24	25–34	35–44	45–54	55–64
average (%)	10.45	6.37	4.81	4.22	4.01
normalized	2.48	1.51	1.14	1	0.95

Notes: data from the CPS, 1976:6–2012:11. The second row indicates average unemployment rates by age, relative to that of 45–54 year olds.

productivity, our model’s declining age profile of separation is because young workers are more likely to be in matches with lower *occupation-specific* productivity. Moreover, our model is consistent with the results of [Kambourov and Manovskii \(2009\)](#) who find that the importance of firm-specific effects in rationalizing life-cycle wage dynamics vanishes when occupation-specific and total experience effects are taken into account in Mincerian wage regressions.<sup>3</sup> In addition, in Section 6, we demonstrate how our model provides a better rationalization of wage dynamics experienced over the life-cycle relative to the firm-specific human capital mechanism.

## 2 Data

In this section, we detail the empirical observations that motivate our work. We first document the large age differences in unemployment. We then present evidence on job finding rates, separation rates, and occupational mobility that informs our theoretical approach in Section 3.

We begin by analyzing the unemployment rate disaggregated by age, obtained from the Current Population Survey (CPS) for the period June 1976–November 2012.<sup>4</sup> The first row of Table 1 displays the average unemployment rate during this period for different age groups. As is obvious, unemployment falls monotonically with age. The average unemployment rate for 20–24 year olds is 10.45% and falls to 4.01% for 55–64 year olds.

Moreover, the age differences are large. The second row presents the average unemployment rate for each age group, relative to that of 45–54 year olds. During this period, average unemployment for 20–24 year olds is 2.48 times that of 45–54 year olds. The average

<sup>3</sup>Using a different methodology, [Pavan \(2011\)](#) argues that while the occupation effect is indeed more prominent than the firm-specific effect, the latter is nevertheless positive.

<sup>4</sup>We focus on this time period since this is the period for which micro-level data (used in the following subsection) is available. None of our substantive results regarding age differences are altered when data from 1948 to 1976 are included.

unemployment rate for 25–34 year olds is 51% greater than that of the prime-aged.

## 2.1 Job Finding and Separation Rates

What accounts for these large age differences? To address this question, we examine the age differences in job finding and separation rates. To understand the role of these transition rates, consider a simple labor market model where: (a) all unemployed workers transit to employment at the constant rate  $f$ , and remain unemployed otherwise, and (b) all employed workers transit to unemployment at the constant rate  $s$ , and remain employed otherwise. In this setting, the steady state unemployment rate,  $u$ , is given by:

$$u = \frac{s}{s + f}.$$

Holding  $f$  constant across age groups, a decreasing age profile for unemployment would require a decreasing profile for  $s$ . Similarly, holding  $s$  constant across age groups, a decreasing age profile for unemployment would require an increasing profile for  $f$ .

We first calculate job finding and separation rates following the approach of [Shimer \(2005\)](#). This approach is well suited for our analysis, since it assumes that all workers transit solely between states of employment and unemployment, as in the statistical model discussed above, and the economic model presented in Section 3.<sup>5</sup> The approach uses monthly data on employment, unemployment, and short-term unemployment tabulated from the CPS. Disaggregated by age, this data is available beginning in June 1976. Panel A of Table 2 displays average job finding and separation rates by age during this period.

The first row of Table 2 indicates that job finding rates decrease monotonically with age. In the average month, 39.54% of unemployed 20–24 year olds transit to employment, a rate that is about 40% greater than that of 45–54 year olds. This represents a small age difference when compared to separation rates, as we discuss below. Moreover, absent differences in separation rates, age differences in job finding rates would counterfactually imply an *increasing* age profile for unemployment.

Hence, age differences in unemployment are accounted for solely by differences in separation rates. The second row of Table 2 indicates that the separation rate falls monotonically with age. Moreover, the age differences are large. For example, the separation rate for 20–24 year olds is 4.0 times that of 45–54 year olds. As such, we view the declining profile of separation rates as integral to any theory of age differences in unemployment.<sup>6</sup>

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<sup>5</sup>We refer the reader to [Shimer \(2005\)](#) for further methodological details.

<sup>6</sup>See also [Topel \(1984\)](#) and [Shimer \(1998\)](#) who emphasize the importance of higher separation rates in

Table 2: Average Monthly Transition Rates by Age Group

	20–24	25–34	35–44	45–54	55–64
<i>A. Shimer approach</i>					
job finding (%)	39.54	34.24	31.17	28.42	27.34
separation (%)	5.58	2.70	1.79	1.39	1.26
<i>B. direct approach</i>					
job finding (%)	28.46	26.58	25.50	23.77	21.35
separation (%)	2.62	1.51	1.13	0.96	0.84

Notes: data from the CPS, 1976:6–2012:11. Panel A presents transition rates computed from data on stocks of employed and unemployed workers. Panel B presents transition rates computed from data on worker flows. See the main text for details.

The [Shimer \(2005\)](#) approach to computing transition rates assumes that workers do not transit in and out of the labor force, though such flows are observed in longitudinal data. This may give rise to misleading conclusions regarding the roles of job finding and separation in rationalizing age differences in unemployment. This is particularly true if transition rates in and out of the labor force differ sufficiently by age.

As such, Panel B of [Table 2](#) displays average transition rates measured directly from data on individual-level labor market flows, using the monthly CPS files. Households in the CPS are surveyed for four consecutive months, then leave the sample during the next eight months, and are surveyed again for a final four months. Since each household member is uniquely identified, we obtain a longitudinal record for each person which allows us to track monthly transitions across states of employment, unemployment, and labor force non-participation.<sup>7</sup>

The first row of Panel B presents the job finding rate (from unemployment to employment). This falls monotonically with age, with the job finding rate of 20–24 year olds about 20% greater than that of 45–54 year olds. Again, these differences alone would counterfactually imply an increasing age profile for unemployment. The second row presents the separation rate (from employment to unemployment). As before, these fall monotonically with age, and the age differences are large. The separation rate for 20–24 year olds is 2.7 times that of 45–54 year olds.<sup>8</sup> Again, this evidence on transition rates indicates the critical

understanding higher unemployment rates for the young.

<sup>7</sup>For a complete description of the construction of the longitudinal data, see [Nekarda \(2009\)](#).

<sup>8</sup>Finally, we note that the levels of transition rates naturally differ across the two measurement approaches, since the previous approach assumes away flows in and out of the labor force. See also [Menzio et al. \(2015\)](#) who study data from the SIPP for male high-school graduates, December 1995 to February 2000. They find

role of separation rates in understanding age differences in unemployment.

## 2.2 Occupational Mobility

The mechanism underlying our theory is that individuals learn about their true calling in life by experiencing various occupations as they age. Following [Kambourov and Manovskii \(2008, 2009\)](#), we use data from the Panel Study of Income Dynamics (PSID) to document the age-profile of occupational mobility.

As is well-known, measures of occupational mobility are subject to sizable measurement error. In order to mitigate this error, the PSID released Retrospective Occupation-Industry Supplemental Data Files (Retrospective Files hereafter) in 1999. The goal of this release was to make available retrospectively assigned 3-digit 1970 census codes to the reported occupations and industries of household heads and wives for the period 1968–80. [Kambourov and Manovskii \(2008, 2009\)](#) argue that the methodology used to construct the Retrospective Files minimizes the error in identifying true occupation switches.<sup>9</sup>

Figure 1 shows the life-cycle profile of occupational mobility rates at the 1-, 2-, and 3-digit level.<sup>10</sup> While the data and methodology underlying Figure 1 comes from [Kambourov and Manovskii \(2008\)](#), we adapt their exercise for the purpose of this study. First, we only use data from the period covered by the Retrospective files. Second, we use a broader sample, consisting of male heads of households who are not self-employed and are either employed or temporarily laid off.<sup>11</sup> The main difference with their sample is our inclusion of government workers and farmers, who tend to switch occupation less frequently than the rest of the sample.

Figure 1 reveals that occupational mobility declines sharply as people age.<sup>12</sup> For the

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that the job finding rate is essentially constant between the ages of 20 and 55, and only fall in a noticeable way between the ages of 55 and 64. Separation rates exhibit a marked fall throughout the age profile, most notably between the ages of 20 and 35, as in the CPS data.

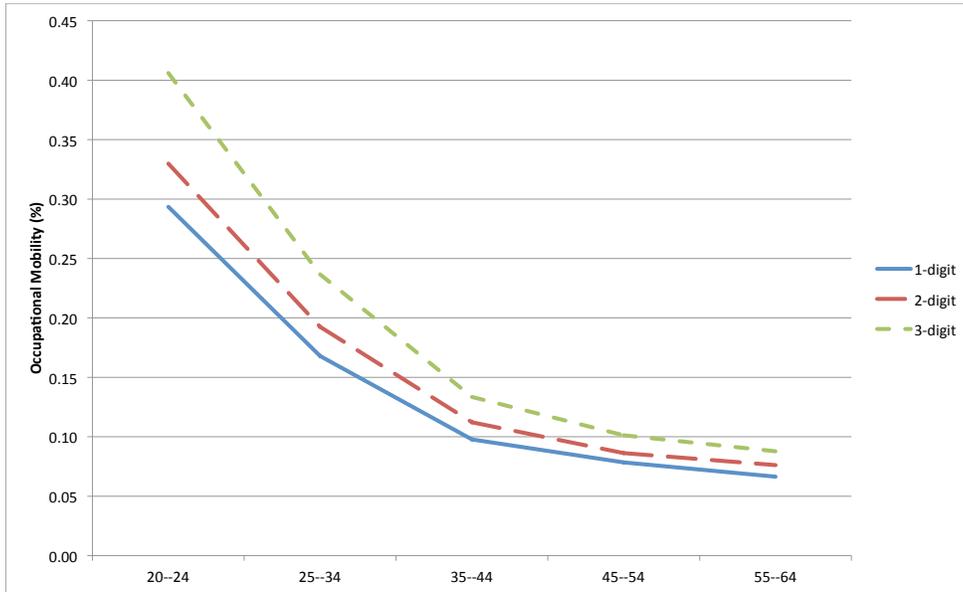
<sup>9</sup>For example, approximately half of occupation switches in the original data are identified as legitimate occupation switches in the Retrospective Files. A key aspect of the Retrospective files is that a single individual was responsible for coding the occupation of a particular individual over the entire sample period, thereby minimizing changes in interpretation of the occupation reported by a given individual over time.

<sup>10</sup>See Appendix B of [Kambourov and Manovskii \(2008\)](#) for details of the occupation classification system.

<sup>11</sup>The latter restriction implies that we do not include individuals who leave the labor force in the calculation of the occupational mobility rate. The mobility rate is the ratio of the number of individuals who switch occupations, divided by the total number of workers (i.e. the sum of ‘switchers’ and ‘non-switchers’). Assume an individual who leaves the labor force (retires or goes to school). If we count this individual as a ‘non-switcher’ we generate a downward bias in the occupational mobility measure (because the denominator is larger). Excluding those who leave the labor force from the sample avoids this bias.

<sup>12</sup>See also [Moscarini and Vella \(2008\)](#) for evidence of declining occupational mobility by in CPS data.

Figure 1: Occupational Mobility by Age



Notes: Data from [Kambourov and Manovskii \(2008\)](#). Original data from the PSID, Retrospective Files, 1968–1980. The sample consists of male heads, non-self-employed, either employed or temporarily laid off.

young, occupational mobility rates are very high: more than 40% of individuals in the 20–24 year old age group switches occupation in a given year at the 3-digit level. Even at the 2-digit level, approximately one in three 20–24 year olds switch occupation annually. For prime-aged workers, about one in 10 or 12 individuals changes 2- or 3-digit occupation on a yearly basis.

These mobility rates can be used to calculate the number of occupations an individual experiences over her working life. For example, suppose that an individual enters the labor force and experiences her first occupation at age 20. Assuming a constant hazard rate between the ages of 20 and 24, the probability that she switches to a different 3-digit occupation during each of the first five years of her career is 41%; this would imply that she switches occupations 2.05 times during the first five years. Similarly, over the next 10 years the average switching probability is 24%, implying 2.40 occupation switches. Repeating this calculation for all the age groups yields that the average worker switches about 8.6 times, and hence works in 9.6 3-digit occupations over her career. A similar procedure indicates that the average person works in 7.3 and 6.6 occupations, at the 2- and 1-digit level, respectively.

Table 3: Rate of Occupational Changes from Unemployment

	Aggregate	20–24	25–34	35–44	45–54	55–64
1-digit (%)	51.24	60.67	50.01	44.42	42.06	39.01
2-digit (%)	55.30	64.81	54.17	48.25	45.88	42.83
3-digit (%)	68.88	77.67	68.68	62.89	60.61	57.35

Notes: data from the CPS, 1994:01–2013:11.

This data supports the notion that individuals learn about their true calling over the life cycle. In the model we present in Section 3, workers who switch occupations do so through intervening spells of unemployment. As such, we proceed by investigating data on occupational mobility *conditional on transiting from unemployment to employment*. To do so, we use the individual-level, matched CPS data during the 1994–2013 period and calculate, among those who transit from unemployment to employment, the fraction whose current occupation differs from the occupation during their previous employment spell.<sup>13</sup> Table 3 displays these statistics at the 1-, 2-, and 3-digit level. A number of results are worth noting.

First, the probability that a worker switches occupations across employment spells when she transits from unemployment to employment is very high. On average, approximately 50% of such transitions involve a 1-digit level occupation switch, and nearly 70% involve a 3-digit occupation switch. We also find that on average, the occupation switching probability from unemployment-to-employment is approximately 16 times that of the occupation switching probability for job-to-job transitions at the 1-digit level, and about 15 times that at the 3-digit level.<sup>14</sup> Most importantly, we find that the rate of occupation switching is decreasing with age: for instance, at the 1-digit level, it falls from about 61% for 20–24 year olds to 39% for 55–64 year olds. Combined with the fact that the young experience much higher separation rates, this evidence is directly supportive of our mechanism: since the young are less likely to have found their true calling (relative to the old), they are also much more likely to experience occupation switching via a spell of unemployment.

<sup>13</sup>Here we use the data beginning in 1994, when the redesign of the CPS significantly improved data quality (due to modifications such as the introduction of dependent coding) regarding occupation classification at the monthly frequency (see [Kambourov and Manovskii \(2013\)](#) and [Moscarini and Thomsson \(2007\)](#)).

<sup>14</sup>Since the pool of employed individuals is much larger than the pool of unemployed individuals, the number of occupational switches from job-to-job is nevertheless non-negligible.

### 3 Economic Environment

To analyze age differences in unemployment, we study a search-and-matching model of the labor market. The matching process between unemployed workers and vacancy posting firms is subject to a search friction. The ratio of vacancies to unemployed determines the economy’s match probabilities, in a way that we make precise in the next subsection.

Workers differ in their knowledge of their best occupational fit. Specifically, there are  $M$  occupations in the economy that are identical, except in name. Each worker is best-suited for one occupation; that is, only one occupation,  $m^* \in \{1, 2, \dots, M\}$ , is a best match, or the worker’s “true calling.” When a worker is employed in her true calling occupation,  $m^*$ , she produces  $f_G$  units of output. For simplicity, in all other  $M - 1$  occupations, the worker-firm pair produces  $f_B$  units of output, with  $f_B < f_G$ .

In each period, a mass of newly born workers enter the economy not knowing their true calling. A new worker has  $m^*$  randomly assigned into one of the  $M$  occupations with probability  $1/M$ . This assignment is distributed independently across all new workers. In order to learn whether any given occupation is their best fit, the worker must search, be matched, and work in that occupation. Learning about occupational fit in a match does not happen instantaneously. In each period of employment, the worker (and firm) learns whether it is the worker’s true calling with probability  $\lambda \in (0, 1)$ .<sup>15</sup>

Given stochastic match creation, destruction, and learning, workers are heterogeneous with respect to their labor market history. Worker heterogeneity can be summarized by a worker’s *type*,  $i \in \{1, \dots, M\}$ ; here,  $i$  indicates the number of ill-suited occupations the worker has identified, plus one. A worker of type  $i < M$  has previously sampled  $i - 1$  ill-suited occupations, and therefore has  $M - i + 1$  left to try; a worker of type  $M$  knows her true calling,  $m^*$  (either having sampled  $M - 1$  ill-suited occupations, or having sampled fewer than that but gotten “lucky”).

Workers understand that their true calling is uniformly distributed across all occupations, and use this to form their beliefs. Hence, an unemployed worker of type  $i = 1$  has a flat prior over occupations, and randomly selects an occupation to search for employment. If that occupation turns out to be the wrong fit, the worker becomes type  $i = 2$  and updates her prior according to Bayes’ rule. She now understands that her true calling is uniformly

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<sup>15</sup>This constant hazard/learning rate can be viewed as the reduced form of a more elaborate signal extraction problem. Specifically, Pries (2004) demonstrates how a model where match output is observed with uniform measurement error gives rise to “all-or-nothing” learning as in our model: with some probability (in our notation,  $1 - \lambda$ ), observed output reveals nothing about the occupational fit, while with complementary probability, the signal is perfectly revealing.

distributed over the remaining  $M - 1$  occupations, and randomly picks one of those occupations to search in the next time she is unemployed. Defining  $\pi_i$  as the probability, conditional on being matched in the  $i^{\text{th}}$  occupation, that the worker has found her true calling, we have that:

$$\pi_i = \frac{1}{M - i + 1}, \quad i = 1, \dots, M.$$

To close the description of the environment, we must take a stand on “death/exit” from the economy. For simplicity, we assume that each worker faces a constant probability of remaining in the labor market from one period to the next,  $\sigma \in (0, 1)$ . We interpret  $\beta$  in what follows as the “true” discount factor times this survival probability.

### 3.1 Market Tightness

We assume that there are  $M$  labor markets in the economy, one for each occupation. All unemployed workers seeking employment in a particular occupation search in that occupation’s market.

While a worker’s type is known to the worker, it is unobservable by vacancy posting firms. Workers are unable to signal their type to potential employers. A firm wishing to hire a worker in a particular occupation posts a vacancy in that occupation’s market, understanding that it may be matched with a worker of any type  $i \in \{1, \dots, M\}$ . The probability the firm assigns to being matched with a type  $i$  worker is taken parametrically, and determined by the equilibrium distribution of unemployed worker types. In this sense, matching is *random* within each occupational market.<sup>16</sup> Upon matching, the worker’s type is observable by both the worker and firm.

Given the symmetry assumptions of the model, all occupational markets are identical. We define market tightness in the representative market,  $\theta$ , as the ratio of the number of vacancies maintained by firms to the number of workers looking for jobs in that occupation. While  $\theta$  is an equilibrium object, it is taken parametrically by firms and workers.

We denote the probability that a worker will meet a vacancy—the job finding rate—by  $p(\theta)$ , where  $p : \mathcal{R}_+ \rightarrow [0, 1]$  is a strictly increasing function with  $p(0) = 0$ . Similarly, we let  $q(\theta)$  denote the probability that a firm with a vacancy meets a worker, where  $q : \mathcal{R}_+ \rightarrow [0, 1]$  is a strictly decreasing function with  $q(\theta) \rightarrow 1$  as  $\theta \rightarrow 0$ , and  $q(\theta) = p(\theta)/\theta$ .

Finally, we note that this structure of matching markets implies that all unemployed workers face the same job finding rate. This feature allows us to isolate the role of occu-

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<sup>16</sup>See also [Pries \(2008\)](#) who studies a model with random search and heterogeneous workers.

pational learning in generating heterogeneity in separation rates. We find this to be an attractive feature of our approach, since age differences in separation fully account for age differences in unemployment, as discussed in Subsection 2.1.

### 3.2 Contractual Arrangement and Timing

We specify the worker’s compensation in a match as being determined via Nash bargaining with fixed bargaining weights, as in Pissarides (1985). When an unemployed worker and a firm match, they begin producing output in the following period. In all periods that a worker and firm are matched, the compensation is bargained with complete knowledge of the worker’s type.

### 3.3 Worker’s Problem

Workers can either be unemployed or employed. Employed workers can either be: in a “good” match, working in their true calling occupation; in a “bad” match, in an occupation that is not the worker’s true calling; or in a match of yet unknown occupational fit.

We define  $U_i$  as the value of being unemployed for a worker of type  $i$ :

$$U_i = z + \beta [p(\theta)W'_{L,i} + (1 - p(\theta))U'_i], \quad i = 1, \dots, M - 1. \quad (1)$$

Here,  $z$  is the flow value of unemployment,  $W_{L,i}$  is the worker’s value of being employed in her  $i^{th}$  occupation and learning whether it is her true calling, and primes ( $'$ ) denote variables one period in the future. An unemployed worker transits to employment in the following period with probability  $p(\theta)$ .

Once employed, the type  $i$  worker’s value while in the “learning phase” is given by:

$$W_{L,i} = \omega_{L,i} + \beta(1 - \lambda) [(1 - \delta)W'_{L,i} + \delta U'_i] + \beta\lambda [\pi_i ((1 - \delta)W'_M + \delta U'_M) + (1 - \pi_i) ((1 - \delta)W'_{B,i} + \delta U'_{i+1})]. \quad (2)$$

While employed in a match of unknown occupational fit, the worker earns per period compensation  $\omega_{L,i}$ , and learns whether this is her true calling with probability  $\lambda$ . If the worker does not learn, then she remains as type  $i$  in the following period. If the match separates, with exogenous probability  $\delta \in (0, 1)$ , she returns to being unemployed with value  $U_i$ ; otherwise, she continues with value  $W_{L,i}$ .

If the worker does learn about her fit in the current occupation, her continuation value is given by the square bracketed term in the second line of equation (2). With probability

$\pi_i$ , the worker has found her true calling, and she becomes type  $i = M$ . Otherwise, the current occupation is not her true calling. If the match does not exogenously separate, she continues as a worker in a bad occupational match with value  $W_{B,i}$ ; if the match separates, she becomes unemployed of type  $i + 1$ , having eliminated an additional occupation as her true calling.

The worker's value of being employed in her true calling is given by:

$$W_M = \omega_M + \beta [(1 - \delta)W'_M + \delta U'_M]. \quad (3)$$

Obviously, if the match exogenously separates, the worker retains her type  $M$  as she knows her true calling; in this case, the value of being unemployed is:

$$U_M = z + \beta [p(\theta)W'_M + (1 - p(\theta))U'_M]. \quad (4)$$

Finally, the value of being employed in a bad match is given by :

$$W_{B,i} = \max \{ \omega_{B,i} + \beta [(1 - \delta)W'_{B,i} + \delta U'_{i+1}], U_{i+1} \}. \quad (5)$$

Note that the worker chooses either to remain in the match or, if it is preferred, to be unemployed. In the event of separation—whether exogenous or endogenous—the worker becomes unemployed of type  $i + 1$  as she knows that her last occupation was not her true calling.

This formulation assumes that workers will never sample an occupation that they already know is not their true calling. We show later in Proposition 1 that this is indeed a feature of the equilibrium: workers who have sampled  $i$  occupations that are not their best fit never sample one of these again upon separation.

### 3.4 Firm's Problem

Firms—or more correctly, vacancies for a specific occupation—can be either filled or unfilled. When filled, a vacancy may be matched with a worker for whom the occupation is her true calling. In this case, the firm's value is given by:

$$J_M = f_G - \omega_M + \beta [(1 - \delta)J'_M + \delta V'], \quad (6)$$

where  $f_G$  is the output in a true calling match, and  $\omega_M$  is the compensation paid to the worker. In the case of separation, the vacancy becomes unfilled with value  $V$ .

When matched with a type  $i$  worker who is in a bad occupational fit, match output is given by  $f_B$ , and the firm's value is:

$$J_{B,i} = \max \{ f_B - \omega_{B,i} + \beta [(1 - \delta)J'_{B,i} + \delta V'] , V \}. \quad (7)$$

Firms in bad matches may choose to separate if it is in their best interest to do so.

Finally, a firm may be matched with a type  $i$  worker who is learning whether the current occupation is her true calling. We specify the output in a learning match to equal its expected value. This ensures consistency with the expectation used in the firm's determination of vacancy creation, equation (9). In this case, the firm's value is given by:

$$J_{L,i} = \pi_i f_G + (1 - \pi_i) f_B - \omega_{L,i} + \beta \left[ \lambda (1 - \delta) [\pi_i J'_M + (1 - \pi_i) J'_{B,i}] + (1 - \lambda) (1 - \delta) J'_{L,i} + \delta V' \right]. \quad (8)$$

This is composed of the contemporaneous profit (expected match output minus the worker's compensation) plus the continuation value.<sup>17</sup> With probability  $\lambda$ , the worker and firm learn about the occupational fit. With probability  $\pi_i$ , this is the worker's true calling, and (conditional on surviving) the match continues with value  $J_M$ ; otherwise, this is an ill-suited occupational match and the continuation value is  $J_{B,i}$ .

We assume that there is a large number of firms who can potentially post vacancies in any of the  $M$  occupational markets. Doing so requires the payment of a vacancy posting cost,  $\kappa > 0$ . The value of posting a vacancy in the representative market is defined as:

$$V = -\kappa + \beta \left[ q(\theta) \left[ \sum_{i=1}^{M-1} \phi_i J'_{L,i} + \phi_M J'_M \right] + (1 - q(\theta)) V' \right]. \quad (9)$$

An unfilled vacancy is matched with a worker with probability  $q(\theta)$ . Upon filling the vacancy, the firm learns the type of worker that it has matched with. As such, the continuation value, conditional upon matching, is probability weighted across the  $M$  worker types. Here,  $\phi_i$  denotes the firm's probability of matching with a worker of type  $i$ , with  $\sum_{i=1}^M \phi_i = 1$ .

## 4 Equilibrium

### 4.1 Definition of Equilibrium

A stationary equilibrium with Nash bargaining is a collection of value functions  $\left( \{J_{B,i}, J_{L,i}\}_{i=1}^{M-1}, J_M, V; \{U_i, W_{B,i}, W_{L,i}\}_{i=1}^{M-1}, U_M, W_M \right)$ , compensations  $\left( \{\omega_{L,i}, \omega_{B,i}\}_{i=1}^{M-1}, \omega_M \right)$ , a proba-

<sup>17</sup>As discussed in footnote 12, our model is isomorphic to one in which output in the learning phase of a match is observed with measurement error.

bility distribution over unemployed workers  $\{\phi_i\}_{i=1}^M$ , and a tightness ratio  $\theta$  such that:

1. workers are optimizing:  $W_{L,i} > U_i, W_{B,i} \geq U_{i+1}, i = 1, \dots, M-1$ , and  $W_M > U_M$ ;
2. firms are optimizing:  $J_{L,i}, J_M > V, J_{B,i} \geq V, i = 1, \dots, M$ ;
3. compensations solve the generalized Nash bargaining problems displayed below;
4. the probability distribution over unemployed workers is consistent with individual behavior and the implied laws-of-motion across labor market states and worker types (see the Appendix for details); and
5. the free entry condition is satisfied. That is,  $V = 0$ .

## 4.2 Compensation

As is standard in the literature, we assume that compensation is determined via generalized Nash bargaining. Let  $\tau$  denote the bargaining weight of workers. The compensation earned by workers in good matches solves the following problem:

$$\omega_M = \arg \max (W_M - U_M)^\tau (J_M)^{1-\tau}.$$

The solution takes the form:

$$\omega_M = \tau f_G + (1 - \tau) [z + p(\theta)\beta(W'_M - U'_M)].$$

The interpretation of this is standard. In a good match, the worker is paid a fraction,  $\tau$ , of the match output, plus a fraction,  $1 - \tau$ , of the value of unemployment. The value of unemployment consists of both the flow value,  $z$ , and the *option value* of being unemployed.

The compensation for workers who are in their  $i^{th}$  bad match solves:

$$\omega_{B,i} = \arg \max (W_{B,i} - U_{i+1})^\tau (J_{B,i})^{1-\tau}.$$

For these workers, the outside option of remaining in the match is being unemployed of type  $i + 1$ . As such:

$$\omega_{B,i} = \tau f_B + (1 - \tau) [z + p(\theta)\beta(W'_{L,i+1} - U'_{i+1})].$$

Finally, the compensation for type  $i$  workers in a learning-phase match solves:

$$\omega_{L,i} = \arg \max (W_{L,i} - U_i)^\tau (J_{L,i})^{1-\tau}.$$

For these workers, the threat point is  $U_i$ : if agreement is not reached in bargaining, they return to unemployment having not learned anything about their type. The solution for  $\omega_{L,i}$  is given by:

$$\begin{aligned} \omega_{L,i} = & \tau [\pi_i f_G + (1 - \pi_i) f_B] + (1 - \tau) [z + p(\theta) \beta (W'_{L,i} - U'_i)] \\ & - (1 - \tau) \beta \lambda [\pi_i U'_M + (1 - \pi_i) U'_{i+1} - U'_i]. \end{aligned}$$

Relative to  $\omega_M$  and  $\omega_{B,i}$ ,  $\omega_{L,i}$  contains a new term,  $\beta \lambda [\pi_i U'_M + (1 - \pi_i) U'_{i+1} - U'_i]$ . We refer to this as the *information value*. By working in the match, the worker learns about her fit in the current occupation with probability  $\lambda$ . Conditional on learning, she learns that it is her true calling with probability  $\pi_i$ ; with complementary probability she learns that her type (when next unemployed) is  $i + 1$ . Hence, the information value is the discounted, expected gain to working and augmenting her threat point in future bargaining.

Moreover, the information value is *positive*. This follows as an immediate corollary of Proposition 1, which we establish below. Hence, the information value term represents a “pay cut” to the worker relative to the standard Nash bargaining solution. Because the worker has this additional incentive to work—to advance toward her true calling—she is willing to accept this pay cut in her negotiated compensation.

### 4.3 Characterizing Equilibrium

In this section we establish that in any stationary equilibrium, the value of unemployment increases with workers’ type, that is,  $U_i < U_{i+1}$ ,  $i = 1, \dots, M - 1$ . This result is useful not only as it leads to a sharp characterization of stationary equilibria, but also because unemployed workers in such equilibria have an incentive to become informed about their type or true calling.

**Proposition 1** *Assume that all bad matches endogenously separate.<sup>18</sup> In any stationary equilibrium,  $U_i < U_{i+1}$  for  $i = 1, 2, \dots, M - 1$ .*

The proof is contained in the Appendix. A number of results follow immediately from this Proposition, collected in the following Corollary:

**Corollary 1** *Assume that all bad matches endogenously separate. Then*

1.  $J_{L,i+1} > J_{L,i}$ ;

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<sup>18</sup>This assumption holds in all equilibria we compute in Section 5.

2.  $W_{L,i+1} - U_{i+1} > W_{L,i} - U_i$ ;
3.  $W_{L,i+1} - W_{L,i} > U_{i+1} - U_i > 0$ , so  $W_{L,i+1} > W_{L,i}$ ;
4.  $\pi_i U_M + (1 - \pi_i) U_{i+1} - U_i > 0$ .

## 5 Numerical Analysis

In Subsection 5.1, we discuss the calibration of our model to the U.S. data. Subsection 5.2 presents results regarding our model’s ability to match the life-cycle labor market facts, and Subsection 5.3 discusses robustness.

### 5.1 Calibration

Many of our model features are standard to the DMP literature, so our strategy is to maintain comparability wherever possible. The model is calibrated to a monthly frequency. As such, the discount factor is set to  $\beta = 0.996$  to accord with an annual risk free rate of 5%.

We assume that the matching function in each occupational market is Cobb-Douglas:

$$p(\theta) = \theta q(\theta) = \theta^\alpha.$$

Summarizing a large literature that directly estimates the matching function using aggregate data, [Petrongolo and Pissarides \(2001\)](#) establish a plausible range for  $\alpha$  of 0.3 – 0.5. Refining the inference approaches of [Shimer \(2005\)](#) and [Mortensen and Nagypál \(2007\)](#), [Brügemann \(2008\)](#) obtains a range of 0.37–0.46. In our calibration, we specify  $\alpha = 0.4$  to be near the mid point of these ranges (see also [Pissarides \(2009\)](#)). For comparability with previous work, we specify the parameter in the Nash bargaining problem as  $\tau = 1 - \alpha$ .

To calibrate  $\delta$  and  $\kappa$ , we target two aggregate moments. First, we set the aggregate unemployment rate among the model’s 20 to 64 year old workers to equal 5.75%. This corresponds to the average aggregate unemployment rate observed among 20–64 year olds in the the CPS data, between 1976:6 to 2012:11. Second, we set the aggregate job finding rate to equal 38.5% to match the job finding rate observed during the same time period in the U.S. data. These two moments pin down the parameter values to be  $\delta = 0.012$  and  $\kappa = 0.234$ .<sup>19</sup>

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<sup>19</sup>More precisely, we normalize  $\theta$  to one, and use a match efficiency parameter  $\eta$  in the matching technology, so that  $p(\theta) = \eta\theta^\alpha$ , with  $\eta = 0.385$ . For any value of  $\delta$ , then, the free entry condition implies a value for  $\kappa$ . We then iterate on  $\delta$  until the model replicates an unemployment rate of 5.75% among the 20–64 year olds.

The model’s aggregate unemployment rate depends on the age distribution of endogenous separation rates. This, in turn, depends on the model’s age distribution of workers. As such, we set the labor market survival probability,  $\sigma$ , to best match the age distribution of the labor force observed in the data. Specifically, we minimize the sum of squared residuals between the model implied labor force shares in the 20–24, 25–34, 35–44, 45–54, and 55–64 age bins, with the average values of those shares in the CPS data, 1976:6 to 2012:11. This results in a value of  $\sigma = 0.9984$ .<sup>20</sup> As an additional check, we find that this survival probability implies an average worker age of 39.02 years in the model, which matches exactly (to the second decimal place) the average age found in the data.

Our calibration of  $z$ , the flow value of unemployment, follows the strategy of [Hall and Milgrom \(2008\)](#), [Mortensen and Nagypál \(2007\)](#), and [Pissarides \(2009\)](#). Specifically, we interpret  $z$  as being composed of two components: a value of leisure or home production, and a value associated with unemployment benefits. As in their work, the return to leisure/home production is equated to 43% of the average return to market work. Given this target, the model’s Nash bargained compensation, and the steady state distribution of worker types, we set  $z = 0.56$ . This implies an unemployment benefit replacement rate of 35% for the lowest type ( $i = 1$ ) workers, and 20% for the highest type ( $i = M$ ) workers; this accords with the range of replacement rates reported by [Hall and Milgrom \(2008\)](#).

In the model exposition of Section 3, we defined  $M$  as the total number of occupations in the economy. Taking this literally would imply an unreasonably large value; for instance, there currently are approximately 500 census occupation codes at the 3-digit level. A more nuanced reading of the model reveals that  $M$  is the number of occupations an individual views as being in her set of potential “best fits” with her skills/tastes when she first enters the labor market.<sup>21</sup> Since,  $M$  is clearly not observable, we calibrate it based on the data on occupational mobility of [Kambourov and Manovskii \(2008\)](#). Taking the age profile of occupational switching rates as hazard rates implies that the average individual works in 9.6 three-digit occupations over her career. Matching this statistic in our model would require  $M = 19$ ; defining occupations at the 1-digit level would imply setting  $M = 13$ . However, this interpretation of the occupational mobility data might overstate our model’s ability to match age difference in separation; this occurs if some of observed occupational

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<sup>20</sup>The exact age distribution generated by the model is discussed in detail in subsection 6.1.

<sup>21</sup>Under this interpretation, individuals are homogenous in  $M$  but can be heterogeneous in the identities of those  $M$  occupations. In this way, the model can be rationalized with the many ( $> M$ ) occupations observed in the data; all that is required is that the distribution of occupation identities across the continuum of individuals’ choice sets is consistent with the distribution of agent types within an occupation, so that the firm’s value of vacancy creation satisfies equation (9).

switches happen without an intervening spell of unemployment, such as internal promotions for example. Given this, we choose to be conservative and set  $M = 10$  in our baseline calibration, so that the average worker experiences 5 occupations over her career.<sup>22</sup>

Relative to the standard DMP model, our model emphasizes the role of learning about one’s true calling that occurs through the sampling of occupations. Knowledge about occupational fit represents a form of human capital that is acquired through labor market experience. Given this, it is natural to calibrate the remaining novel parameters of our model— $f_G$ ,  $f_B$ , and  $\lambda$ —to match the empirical life-cycle earnings profile, as estimated by [Murphy and Welch \(1990\)](#) and others. That is, in our baseline calibration, we assume that the returns to occupational learning match exactly the returns to labor market experience.

We choose  $f_G/f_B$  and  $\lambda$  to match two key properties of the return to experience. First, the maximal lifetime wage gain for a typical worker represents an approximate doubling of earnings. Second, this doubling occurs after the typical worker has accumulated 25 years of experience. Normalizing  $f_G = 1$  and matching these statistics in our model requires setting  $f_B = 0.57$  and  $\lambda = 1/18$ .<sup>23</sup> This implies that a worker’s match productivity is 75% higher in her true calling than in any other occupation, and that it takes, on average, 18 months in a match in order to learn the occupational fit.

In our results, we assume that workers are “born” into the workforce at the age of 19.5 years old. We allow 6 months to elapse before tracking labor market outcomes, so that the youngest worker in the age-specific statistics we report is 20 years old. Results for the baseline calibration are contained in the next subsection, and robustness of our results to variation in  $M$ ,  $f_G/f_B$ , and  $\lambda$  is investigated following that.

## 5.2 Results

The first row of Panel A, [Table 4](#) reproduces the unemployment rate by age displayed in [Table 1](#). The second row displays the age profile of unemployment generated by the baseline calibration of our model. Occupational learning over the life cycle implies that unemployment falls as workers age and find their true calling. Through this mechanism,

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<sup>22</sup>We note that [Topel and Ward \(1992\)](#) find that the typical male high school graduate holds approximately 10 or 11 jobs throughout his career. Given the different datasets, time periods, and sample selection criteria employed, their statistics on job mobility need not correspond with ours on occupational mobility. Nonetheless, it is worth noting the similarity in mobility, and that the number of jobs exceeds the number of occupations (since not all job changes involve an occupation change).

<sup>23</sup>Technically, given the non-deterministic nature of our model, the expected life-cycle profile of earnings only asymptotes to the theoretical maximal value as time approaches  $\infty$ . Hence, our calibration procedure requires that earnings come within 0.25% of fully doubling at the 25 year horizon.

Table 4: Labor Market Statistics by Age Group: Data and Model

	20–24	25–34	35–44	45–54	55–64
<i>A. unemployment rate</i>					
U.S. data (%)	10.45	6.37	4.81	4.22	4.01
model (%)	12.21	7.33	3.58	3.06	3.04
<i>B. separation rate</i>					
U.S. data (%)	5.58	2.70	1.79	1.39	1.26
model (%)	5.33	3.03	1.42	1.21	1.20

Notes: U.S. data from the CPS. Model statistics computed from the theoretical steady state distribution of the baseline calibration.

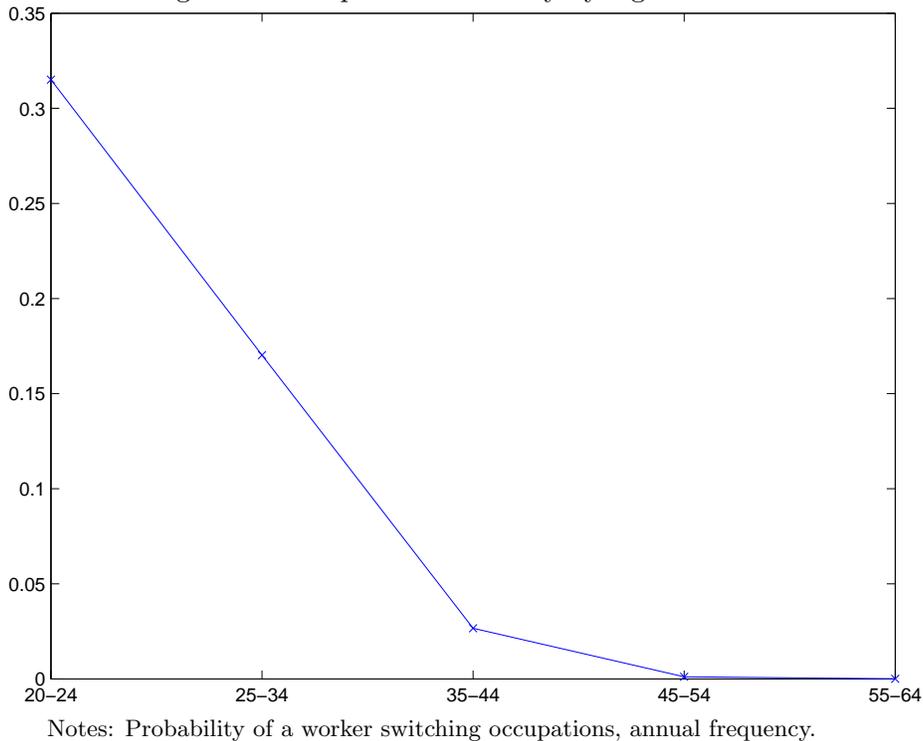
our model does a very good job at matching the observed age profile of unemployment.

The assumption of random search within an occupational market implies that the job finding rate of all workers is identical. As such, all age differences in unemployment are driven by differences in separation rates. In our model, separation rates differ across workers because they face different endogenous separation probabilities. In our baseline calibration, all workers choose to separate if they learn that their current match is of poor occupational fit. That is,  $W_{B,i} = U_{i+1}$  for all  $i = 1, \dots, M - 1$  in equation (5). Only type  $i = M$  matches separate at the exogenous rate  $\delta$ ; all other matches—namely, learning-phase matches—separate at rate  $\delta + (1 - \delta)\lambda(1 - \pi_i) > \delta$ . Hence, our model obtains a declining age profile of separation because older workers are more likely to have found their true calling.

This can be seen in Panel B of Table 4 where we display separation rates by age.<sup>24</sup> In the baseline calibration of our model, young workers aged 20–24 years old tend not to have found their true calling; as such, they face a separation rate of 5.33%. On the other hand, old workers aged 55–64 have essentially all found their true calling; their separation rate of 1.20% is essentially identical to the calibrated exogenous separation rate,  $\delta$ . Moreover, our model does a good job of accounting for the age profile of separation rates. For example, the separation rate of 20–24 year olds is 4.4 times that of either the 45–54 or 55–64 year olds. In the U.S. data, this ratio is 4.0 and 4.4, respectively. Hence, the reason our model overstates age differences in unemployment rates is because of our simplifying assumption of identical job finding rates.

<sup>24</sup>For the U.S. data, we report separation rates as calculated in Shimer (2005), as this method accords with our model’s assumption that workers do not transit in and out of labor force participation during their working-age life.

Figure 2: Occupational Mobility by Age: Model



Finally, we note that our model does a good job of replicating the age profile of occupational mobility. Figure 2 displays the occupational switching rate at the annual frequency for different age groups in our model; this is analogous to Figure 1 derived from the PSID data studied by [Kambourov and Manovskii \(2008\)](#). For young workers aged 20–24 years old, the model generates an occupational switching rate of 32% which is very close to the rate found at the 2-digit occupational level in the data. However, occupational mobility falls faster in the model relative to the data: by the time workers reach prime age, essentially everyone has found their true calling, and the occupational switching rate is near zero. We address this shortcoming in an extension of the model presented in Section 6.

### 5.3 Robustness

Here we explore the robustness of our results to variations from the baseline calibration. We first consider the effect of changing  $M$ , the number of potential occupations. To see that  $M$  affects the ability to generate age differences in unemployment, consider the case of  $M = 1$ : the model collapses to the standard representative worker DMP model (augmented with a constant survival probability).

Table 5: Labor Market Statistics by Age Group: Robustness

	20–24	25–34	35–44	45–54	55–64
<i>A. U.S. data</i>					
unemployment rate	10.45	6.37	4.81	4.22	4.01
separation rate	5.58	2.70	1.79	1.39	1.26
<i>B. benchmark model</i>					
unemployment rate	12.16	7.30	3.57	3.04	3.02
separation rate	5.33	3.03	1.42	1.21	1.20
<i>C. <math>M = 7</math></i>					
unemployment rate	11.71	6.10	3.99	3.91	3.91
separation rate	5.11	2.50	1.60	1.57	1.57
<i>D. <math>M = 13</math></i>					
unemployment rate	12.12	8.14	3.77	2.31	2.18
separation rate	5.31	3.41	1.51	0.91	0.86
<i>E. <math>\lambda = 1/12</math></i>					
unemployment rate	14.87	6.30	3.02	2.96	2.96
separation rate	6.72	2.59	1.20	1.17	1.17

Notes: U.S. data from the CPS. Model statistics computed from the theoretical steady state distribution for various parameter specifications.

Panels C and D of Table 5 address this exercise. First, we reduce the number of occupations to  $M = 7$ ; this accords with the implied number of 1-digit occupations worked by the average individual using the PSID data. Doing so reduces the amount of time a worker spends over her life cycle searching for her true calling. In these results, the rest of the parameter values are reset to maintain the remaining calibration targets discussed in Subsection 5.1.<sup>25</sup>

Despite the 30% reduction in the number of potential occupations, the model still delivers sizable age differences in unemployment and separation. Young workers in the model experience an unemployment rate that is 3.0 times that of 45–54 year olds. In terms of separation rates, the model delivers a ratio of 20–24 year olds to 45–54 year olds of 3.25, close to the ratio of 4.0 observed in the data. For similar reasons, Panel D of Table 5 shows that increasing the number of potential occupations to  $M = 13$  amplifies the age differences in unemployment and separation rate.

<sup>25</sup>Specifically, we keep targeting the same job finding rate of 38.5% by recalibrating  $\kappa$ , and set  $\delta$  so that we have a 5.75% working-age unemployment rate. I.e. the logic of this approach enables to answer what would the results of our model be if we had  $M = 7$  as the benchmark case.

In our second robustness exercise, we increase the learning rate to  $\lambda = 1/12$ . This represents a 50% increase in the learning rate relative to the baseline calibration, and implies that workers learn their occupational fit in a match in 12 months, on average. Increasing  $\lambda$  has the effect of reducing the amount of time a worker spends over her life cycle searching for her true calling. The results are displayed in Panel E of Table 5.

Not surprisingly, increasing  $\lambda$  causes workers to spend more of the early part of their career unemployed, as they transition between occupations. Relative to the baseline calibration, the unemployment and separation rates of 20–24 year olds are 25% higher. Beyond this age group, workers are more likely to have found their true calling, and age differences in unemployment and separation rates among 25 to 64 year old workers are compressed compared to the baseline calibration.

Finally, we note that our main results are essentially unaffected by the value of  $f_B$  relative to  $f_G$  (recall that we normalize  $f_G = 1$ ). This follows from the fact that the allocation is invariant to this ratio as long as matches endogenously separate when an occupation is revealed to be a poor fit. Under our benchmark calibration, increasing  $f_B$  relative to  $f_G$  has no impact on the unemployment nor the separation rates as long as  $f_B/f_G < 0.92$ .<sup>26</sup> This invariance result can be derived analytically, and can be demonstrated simply for the case when  $M = 2$ .<sup>27</sup> In this case, bad matches endogenously separate as long as

$$f_B < z + \beta p(\theta)\tau \left[ \frac{f_G - z}{1 - \beta(1 - \delta - p(\theta)\tau)} \right],$$

highlighting that equilibrium allocations are invariant as long as  $f_B$  satisfies a cutoff rule.

## 6 Applications

Here we consider two applications of our model. These illustrate how the basic life-cycle mechanism linking job separation, unemployment, and occupational mobility can account for a number of novel labor market phenomena, at both the individual- and macro-levels.

### 6.1 Labor Force Aging and Aggregate Unemployment

The empirical results of Shimer (1998) indicate that the age composition of the labor force has a causal impact on the level of aggregate unemployment. Specifically, the entrance of

<sup>26</sup>While the allocation is invariant to changes in  $f_B/f_G$  in the relevant range, such is obviously not the case for wages.

<sup>27</sup>The general proof, for  $M \geq 2$ , is available from the authors upon request.

the postwar baby boom generation into the workforce in the mid- to late-1970’s and their subsequent aging accounts for a substantial fraction of the rise and fall in U.S. unemployment observed in the past 50 years. In this subsection, we address this issue within the context of our structural model of life-cycle unemployment. We determine what fraction of the observed change in aggregate unemployment can be accounted for by the “learning about occupational fit” mechanism embodied in our analysis.

Specifically, we keep all parameters of the model identical to the benchmark calibration, except for the value of the labor market survival probability,  $\sigma$ . As discussed in subsection 5.1,  $\sigma$  determines the model’s age distribution of the labor force. By varying this parameter, we are able to “tilt” the age distribution to resemble that of the late-1970’s, when the baby boom first entered the labor force, and compare the resulting unemployment rate predictions to those when the age distribution resembles the recent period.

Panel A of Table 6 replicates the U.S. data averaged over the 1976:6–2012:11 period, as well as results for the model calibrated to this time period, as presented in Table 4. It also provides additional information pertaining to the age distribution of the labor force. Given that the model has only one parameter,  $\sigma$ , to match the age distribution, the benchmark calibration does a surprisingly good job at replicating the U.S. data.

The first two rows of Panel B present U.S. data averaged over 1976–1983, a period featuring the entrance of the baby boom generation to the workforce. This is evidenced by the larger share of the labor force aged 34 years and younger, relative to 1976–2012 as a whole. This early period is also marked by higher aggregate unemployment.

Since this is a short, eight year time period, a simple time-series average of the unemployment rate is unlikely to eliminate the effects of business cycle fluctuations. This is particularly true since 1976–1983 featured many years of recession and relatively few “boom” years. As a result, we use the HP filter to eliminate the cyclical component of the unemployment data.<sup>28</sup> Given our interest in “steady state” analysis and the impact of low-frequency change in demographics, we present the average unemployment rate of the HP filtered trend. As the rightmost column of Table 6, Panel B indicates, aggregate unemployment was high in this period: 6.59%, as compared to 5.75% during 1976–2012. This is true of each age-specific unemployment rate as well.

The bottom two rows of Panel B present results from our model calibrated to this time period. In particular, we lower the survival probability to  $\sigma = 0.9978$  in order to minimize

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<sup>28</sup>Since the HP filter performs poorly near the endpoints of time series, we extend the unemployment rate data to 1950 before applying the filter.

Table 6: Labor Market Statistics by Age Group: Counterfactual

	20–24	25–34	35–44	45–54	55–64	20–64
<i>A. 1976–2012</i>						
<i>U.S. Data</i>						
labor force share	12.90	27.90	25.88	21.01	12.31	100
unemployment rate	10.45	6.37	4.81	4.22	4.01	5.75
<i>Model</i>						
labor force share	15.68	27.29	22.65	18.79	15.59	100
unemployment rate	12.21	7.33	3.58	3.06	3.04	5.75
<i>B. 1976–1983</i>						
<i>U.S. Data</i>						
labor force share	16.77	30.50	21.69	18.27	12.78	100
unemployment rate	11.87	7.22	5.01	4.37	4.04	6.59
<i>Model</i>						
labor force share	17.77	29.23	22.47	17.27	13.27	100
unemployment rate	12.57	7.60	3.71	3.15	3.13	6.25
<i>C. 2002–2009</i>						
<i>U.S. Data</i>						
labor force share	10.95	23.75	26.05	25.16	14.10	100
unemployment rate	9.75	5.80	4.53	4.01	3.84	5.17
<i>Model</i>						
labor force share	13.29	24.80	22.59	20.58	18.74	100
unemployment rate	11.96	7.13	3.50	2.99	2.98	5.32

Notes: U.S. data from the CPS. Model statistics computed from the theoretical steady state distribution for various parameter specifications.

the sum of squared residuals between the model’s labor force shares in each of the five age bins with the average values observed in the data. As a check, we find that this value of  $\sigma$  implies an average worker age of 37.85 years in the model as compared to an average age of 37.90 in the U.S. data.

Panel B indicates that the model does well in replicating the higher aggregate unemployment rate observed during this period. Lowering  $\sigma$  to match the younger labor force composition raises the 20–64 year old unemployment rate to 6.25%. This is close to the value of 6.59% found in the data.

Panel C of Table 6 presents results for the period 2002–2009. Obviously, the labor force is noticeably older given the aging of the baby boom. The aggregate unemployment rate is

also noticeably lower.<sup>29</sup> The bottom rows present results from the model. To best match the labor force age distribution during this period, we set  $\sigma = 0.9992$ . This implies an average worker age of 40.50 in the model as compared to 40.54 in the U.S. data. Again, the model does a good job of accounting for observed unemployment. Aging of the workforce causes the aggregate unemployment rate to fall to 5.32%, as compared to 5.17% in the data.

Hence, aging of the labor force—in a manner that best matches that observed from the mid-1970’s to present—causes aggregate unemployment to fall by 0.93% in our model.<sup>30</sup> This compares with a fall of 1.42% in the U.S. data. As such, the model rationalizes 65% of the observed change in aggregate unemployment.

The changes in aggregate unemployment rates shown in Table 6, both for the actual and the model-generated data, can be decomposed into two components: one that is “mechanical,” due simply to changes in labor force shares, and an equilibrium or “behavioral” response. Comparing the age-specific unemployment rates across Panels B and C highlights that the change in aggregate unemployment generated by the model is not simply mechanical. As the labor force ages, the unemployment rate of 20–24 year olds falls from 12.57% to 11.96%; the unemployment rate of 45–54 year olds falls from 3.15% to 2.99%. Indeed, this behavioral implication of our model is consistent with the U.S. data: labor force aging has been accompanied by lower unemployment rates for workers of all age groups.

In our model, this equilibrium effect on unemployment operates through the free entry condition (equation (9)). As the labor force ages, the endogenous distribution of unemployed worker types shifts, so that there are fewer low-type workers, and more workers who know their true calling. Hence, for any given vacancy cost,  $\kappa$ , firms are willing to create more vacancies per unemployed worker, since the expected surplus from a match is greater.<sup>31</sup> This results in a higher job finding rate, and lower unemployment rate, among all workers.

Indeed, it is possible to quantify the relative importance of the two effects on the unemployment rate change generated by the model. The mechanical component takes the age-specific unemployment rates in Panel B, and weights them by the 2002–2009 labor force shares of Panel C, implying an aggregate unemployment rate of 5.63%. Hence, of the

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<sup>29</sup>Again, given the poor performance of the HP filter at endpoints of time series, we have chosen to end our analysis period in 2009, and not consider the filtered data from the last three years of the sample. Including the data from the Great Recession would increase the observed unemployment rates. Given our calibrated results, discussed shortly, this would improve the model’s ability to explain the observed unemployment rate changes via demographic change.

<sup>30</sup>As a point of reference, our results are similar to the empirical results of [Shimer \(1998\)](#), who finds that aging generates a 1.20% fall in aggregate unemployment from the mid-1970s to the late-1990s.

<sup>31</sup>See also [Pries \(2008\)](#) who emphasizes the importance of compositional change in the pool of unemployed workers in explaining business cycle fluctuations in unemployment.

93 basis point fall in unemployment across the two periods, the mechanical effect of age composition change accounts for  $(6.25 - 5.63) / 0.93 = 67\%$ . The other 33% is due to the equilibrium effect of increased job creation.

Repeating this calculation with the U.S. data reveals that the effect of labor force aging implies a 60 basis point fall between 1976–83 and 2002–09.<sup>32</sup> Given the observed fall in aggregate unemployment, the mechanical component accounts for 43% of the change in the U.S. data. As such, while the model clearly embodies a non-trivial internal propagation mechanism to labor force composition change, it understates the actual behavioral response.

## 6.2 Job Displacement and Occupational Mobility

In this subsection, we consider a simple extension of our model to study the earnings response of workers to job loss. Specifically, we illustrate how this extended model is capable of rationalizing the heterogeneity of responses documented in the empirical literature on “job displacement.” We then discuss how this allows us to compare the empirical relevance of our mechanism relative to that emphasized by [Menzio et al. \(2015\)](#).

Following the seminal work of [Jacobson et al. \(1993\)](#), a number of studies have documented the large and persistent effects of job displacement on earnings and wages, especially for prime-aged workers and those with significant job tenure. We very briefly summarize those findings here.<sup>33</sup> Though, the precise concept of a displacement varies from paper to paper, the common defining feature is that it involves an involuntary job separation. In the period of the separation, the average earnings loss is on the order of 25%; much of this effect is due to the direct effect of lost employment. However, even 5 or 10 years later, the average effect of the displacement on earnings is still negative, indicating that workers tend to earn lower wages when subsequently re-employed.

Relative to this average effect, the literature also documents substantial heterogeneity. For instance, from the Displaced Worker Survey, [Kletzer \(1998\)](#) finds that while a third of re-employed workers earn substantially less than on their pre-displacement job, an equal or larger fraction earn the same or more on their new job. Moreover, [Stevens \(1997\)](#) shows that the displacement effects covary with individual characteristics. Specifically, using data from the PSID, [Stevens \(1997\)](#) finds that large and persistent losses are concentrated among workers who switch occupations across spells of unemployment: wage losses of workers who

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<sup>32</sup>Using a similar methodology for the 16+ population, [Elsby et al. \(2010\)](#) find that the mechanical component accounts for an approximate 100 basis point fall from the 1976–83 period to 2009.

<sup>33</sup>See, for example, [Kletzer \(1998\)](#) for a much more comprehensive survey.

return to the same pre-displacement occupation are less pronounced and recover quickly.<sup>34</sup> Furthermore, those who experience persistent wage losses are also more likely to be those who experience subsequent job losses following the initial displacement.

Our framework emphasizing the relationship between job separation and occupational mobility is well suited to addressing these facts. To begin, note that the benchmark model of Section 3 already rationalizes the substantial fraction of workers who experience re-employment wage gains or negligible wage losses following job separation. This is because a worker’s type is non-decreasing, and wages are increasing in type ( $\omega_M > \omega_{L,i}$  for all  $i < M$ , and  $\omega_{L,j} > \omega_{L,i}$  for  $j > i$ ). To capture occasional large, discrete wage losses, we extend the model by allowing for *occupational displacement* shocks. For simplicity, we assume that only individuals who have found their true-calling (type  $M$ ) are subject to such shocks.

Specifically, we assume that in each period, type  $M$  individuals face a probability,  $\psi$ , that they lose their occupational fit. One interpretation is that from time-to-time, workers lose the skill/taste to perform their true calling occupation. Alternatively, this shock could represent a plant closure or mass layoff that causes a type  $M$  worker’s occupation to disappear or become obsolete in her local labor market. When hit by the displacement shock, the worker’s type is reset: she gets “knocked down” the type ladder to a type  $x < M$ , and must search again for her new true-calling occupation.<sup>35</sup> Given this, the worker switches occupation upon re-employment and experiences a discrete wage loss relative to her previous job. Moreover, given that she is re-employed in an occupation that is likely to be a poor occupational fit, she faces a higher probability of subsequent job separations as she learns about her (new) true calling. All of these features are consistent with the results of Stevens (1997).

For brevity, we discuss only the type  $M$  value functions affected by introducing the occupational displacement shock, and make the remaining details of the model available upon request. The values of being an unemployed and employed type  $M$  worker become:

$$\begin{aligned} U_M &= z + \beta [(1 - \psi) (p(\theta)W'_M + (1 - p(\theta))U'_M) + \psi U'_x], \\ W_M &= w_M + \beta [(1 - \psi) (\delta U'_M + (1 - \delta)W'_M) + \psi U'_x], \end{aligned}$$

where  $U_x$  denotes the value of being unemployed as type  $x$ , and  $x$  is the type to which a worker who has been hit by the shock resets to. Similarly, the value of a firm matched with

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<sup>34</sup>The same result applies to individuals who do not switch industry after job displacement; see also the results of Jacobson et al. (1993).

<sup>35</sup>For example,  $x = 1$  would correspond to a situation where an individual’s labor market experience is irrelevant to identifying her new occupational fit. By contrast,  $x > 1$  would be a situation where an individual’s past experience imparts some knowledge relevant to determining her new true calling.

a type  $M$  worker becomes:

$$J_M = f_G - w_M + \beta [(1 - \psi) ((1 - \delta)J'_M + \delta V') + \psi V'] .$$

To analyze the quantitative implications of this model, we calibrate the two new parameters,  $\psi$  and  $x$ , to key findings from the literature on displaced workers. Kletzer (1998) indicates that approximately one-third of workers experience large wage losses (losses greater than 25%) when they regain employment following a job displacement (i.e., involuntary separation). Data from the Job Openings and Labor Turnover Survey (JOLTS) from 2000:12–2014:11 indicate that around 40% of job separations are involuntary. Since the distinction between various types of separations does not exist in our model, we set  $\psi$  such that 13.3% (one-third of 40%) of workers who become unemployed in any given period experience occupational displacement. We adjust the exogenous separation probability,  $\delta$ , to maintain an aggregate unemployment rate of 5.75% among the working-age population. Finally, we set  $x = M - 3$ . This implies that workers who are displaced experience a 35% wage cut upon re-employment. Moreover, wage losses are persistent: 5 years after separation, wages are on average 10% lower than pre-displacement levels, consistent with the evidence provided by Stevens (1997).

Table 7 displays labor market statistics by age for the extended model, along with the statistics for the U.S. data and benchmark model (originally displayed in Table 4). As is clear, the life-cycle profiles for unemployment and separation rates are very similar to that obtained by the benchmark model; as such, the model extension continues to do a very good job of capturing observed age differences in unemployment and separation.

Figure 3 displays occupational mobility by age in the extended model. While all age-groups are affected by the introduction of occupational displacement, this phenomenon primarily affects prime-age and older workers, since they are most likely to have found their true calling. As a result, more than 6% of workers aged 45 and older switch occupation on an annual basis. This closely resembles the switching rate observed in the PSID data, as shown in Figure 1, and represents a marked increase over the benchmark model, as displayed in Figure 2. Hence, this simple extension of the model is not only consistent with the findings from the job displacement literature, but also improves upon the benchmark model in rationalizing the life-cycle profile of occupational mobility, while simultaneously capturing the life-cycle profile of unemployment.

By contrast, capturing the heterogeneity in earnings responses to job separation in the Menzio et al. (2015) model would be difficult.<sup>36</sup> Recall that in the Jovanovic (1979)

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<sup>36</sup>And obviously, capturing the relationship of wage loss to occupational change would be impossible, since

Table 7: Labor Market Statistics by Age Group with Displacement

	20–24	25–34	35–44	45–54	55–64
<i>A. U.S. data</i>					
unemployment rate	10.45	6.37	4.81	4.22	4.01
separation rate	5.58	2.70	1.79	1.39	1.26
<i>B. benchmark model</i>					
unemployment rate	12.16	7.30	3.57	3.04	3.02
separation rate	5.33	3.03	1.42	1.21	1.20
<i>C. with occupational displacement</i>					
unemployment rate	11.08	6.86	3.95	3.63	3.63
separation rate	4.80	2.84	1.58	1.45	1.45

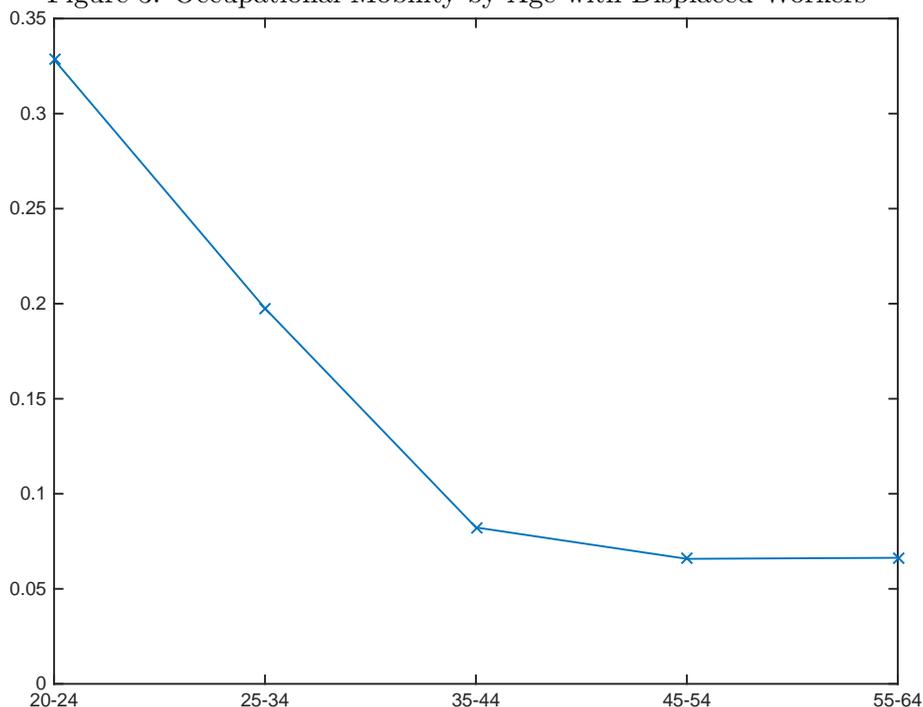
Notes: U.S. data from the CPS. Model statistics computed from the theoretical steady state distribution for various parameter specifications.

and [Menzio et al. \(2015\)](#) framework, human capital is firm-specific. This implies that upon job separation, workers experience a discrete wage change as all human capital is lost. Hence, while large wage losses upon re-employment would be easy to rationalize, the negligible wage effects experienced by a substantial fraction of workers would be hard. It would require displaced workers to be assigned to draw from one of two idiosyncratic match quality distributions upon re-employment: the usual distribution faced by all others, where good draws (leading to high wages and long job tenure) are relatively rare events, and a better one that is reserved for them (i.e. allowing some displaced workers to systematically be more lucky in finding good worker-firm matches). Clearly, admitting this effect into the model would be *ad hoc*, and goes against the spirit of rationalizing age differences in separation rates in a manner that is germane to [Jovanovic \(1979\)](#)'s idiosyncratic match quality mechanism. Thus, the empirical evidence from the job displacement literature allows us to draw a clear distinction between our framework and that of [Menzio et al. \(2015\)](#).

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that model does not consider occupations.

Figure 3: Occupational Mobility by Age with Displaced Workers



Notes: Probability of a worker switching occupations, annual frequency.

## 7 Conclusion

In this paper, we study one of the key life cycle labor market facts: that unemployment declines as a function of age. We propose a simple model of occupational learning that accounts for this fact. Young workers, who are less likely to have found their “true calling,” are more likely to separate from employment matches. Hence, our model correctly predicts that age differences in unemployment rates are due to age differences in separation rates. Our calibrated model does a very good job at quantitatively replicating the age differences in unemployment and separation rates observed in the U.S. data. Moreover, labor force aging in our model accounts for a significant fraction of the fall in aggregate unemployment observed in the past 35 years. Finally, once augmented with the possibility occupational displacement, the model is consistent with several salient facts, namely that displaced workers who switch occupation experience large, persistent wage losses upon reemployment and that these individuals tend to experience several unemployment spells following a displacement. In addition, the extended model produces a life-cycle profile of occupational mobility that closely matches the U.S. data.

## A Distribution of Unemployed Workers

Here we provide details on the distribution of unemployed workers across types. For notational simplicity, we begin with the laws-of-motion for employment and unemployment in steady state.<sup>37</sup> Letting  $u_1$  denote the number of unemployed workers of type 1:

$$u_1 = (1 - \sigma) + \sigma [(1 - p(\theta))u_1 + \delta(1 - \lambda)n_{L,1}],$$

where  $n_{L,1}$  denotes the number of employed workers of type 1 learning about the current occupational fit. In general:

$$n_{L,i} = \sigma [p(\theta)u_i + (1 - \lambda)(1 - \delta)n_{L,i}],$$

for  $i = 1, \dots, M - 1$ .

The number of type  $i$  workers employed in matches of poor occupational fit is given by:

$$n_{B,i} = \sigma [(1 - \delta_{B,i})n_{B,i} + \lambda(1 - \pi_i)(1 - \delta_{B,i})n_{L,i}].$$

Here,  $\delta_{B,i} = 1$  if type  $i$  bad matches endogenously separate, and  $\delta_{B,i} = \delta$  otherwise. The number of unemployed workers of type  $i = 2, \dots, M - 1$  is given by:

$$u_i = \sigma [(1 - p(\theta))u_i + \delta_{B,i-1}n_{B,i-1} + \lambda(1 - \pi_{i-1})\delta_{B,i-1}n_{L,i-1} + (1 - \lambda)\delta n_{L,i}].$$

Finally, for type  $i = M$  workers:

$$n_M = \sigma \left[ (1 - \delta)n_M + p(\theta)u_M + \sum_{i=1}^{M-1} \lambda\pi_i(1 - \delta)n_{L,i} \right],$$

$$u_M = \sigma \left[ (1 - p(\theta))u_M + \delta n_M + \delta_{B,M-1}n_{B,M-1} + \lambda(1 - \pi_{M-1})\delta_{B,M-1}n_{L,M-1} + \delta \sum_{i=1}^{M-1} \lambda\pi_i n_{L,i} \right].$$

Given these definitions:

$$\phi_i = \frac{u_i}{\sum_{j=1}^M u_j}, \quad i = 1, \dots, M.$$

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<sup>37</sup>Out of steady state, variables on the left hand side of all equations would be denoted with a prime ( $'$ ).

## B Proof of Proposition 1

We start by showing that  $U_M > U_{M-1}$ . Assume, by contradiction, that  $U_M \leq U_{M-1}$ . For notational simplicity, we focus on the case of a steady state equilibrium so that  $U'_i = U_i$ ,  $J'_i = J_i$ , etc. From the value of unemployment, we have

$$W_{L,i} - U_i = \frac{(1 - \beta)U_i}{\beta p(\theta)}, \quad i = 1 \dots M,$$

where  $W_{L,M} \equiv W_M$ . So  $U_M \leq U_{M-1}$  implies that  $W_M - U_M \leq W_{L,M-1} - U_{M-1}$ . Using equilibrium wages,

$$\begin{aligned} \omega_M - \omega_{L,M-1} &= \tau(f_G - \bar{f}_{M-1}) + (1 - \tau)p(\theta)\beta[(W_M - U_M) - (W_{L,M-1} - U_{M-1})] + \lambda(1 - \tau)\beta(U_M - U_{M-1}) \\ &= \tau(f_G - \bar{f}_{M-1}) + (1 - \tau)(1 - \beta)(U_M - U_{M-1}) + \lambda(1 - \tau)\beta(U_M - U_{M-1}) \\ &= \tau(f_G - \bar{f}_{M-1}) + (1 - \tau)(1 - \beta(1 - \lambda))(U_M - U_{M-1}). \end{aligned}$$

Now we can write the value of type  $M$  firm as

$$\begin{aligned} J_M &= f_G - \omega_M + \beta(1 - \delta)J_M \pm \beta(1 - \lambda)(1 - \delta)J_M \\ &= \frac{f_G - \omega_M + \beta(1 - \delta)\lambda J_M}{1 - \beta(1 - \lambda)(1 - \delta)}, \end{aligned}$$

and that for type  $M - 1$  as

$$J_{L,M-1} = \frac{\bar{f}_{M-1} - \omega_{L,M-1} + \beta\lambda(1 - \delta)\pi_{M-1}J_M}{1 - \beta(1 - \lambda)(1 - \delta)},$$

where  $\bar{f}_i = \pi_i f_G + (1 - \pi_i) f_B$ . Then we have

$$\begin{aligned} &(1 - \beta(1 - \lambda)(1 - \delta))(J_M - J_{L,M-1}) \\ &= (f_G - \bar{f}_{M-1}) - (\omega_M - \omega_{L,M-1}) + (\beta(1 - \delta) - \beta\lambda(1 - \delta)\pi_{M-1})J_M \\ &= (f_G - \bar{f}_{M-1}) - (\omega_M - \omega_{L,M-1}) + \beta(1 - \delta)\lambda(1 - \pi_{M-1})J_M \\ &= (1 - \tau)(f_G - \bar{f}_{M-1}) - (1 - \tau)(1 - \beta(1 - \lambda))(U_M - U_{M-1}) + \beta(1 - \delta)\lambda(1 - \pi_{M-1})J_M, \end{aligned}$$

that is,  $J_M > J_{L,M-1}$ . This is a contradiction of Nash bargaining: since  $\tau J_M = (1 - \tau)(W_M - U_M)$  and  $\tau J_{L,M-1} = (1 - \tau)(W_{L,M-1} - U_{M-1})$ , we have

$$0 < \tau[J_M - J_{L,M-1}] = (1 - \tau)[(W_M - U_M) - (W_{L,M-1} - U_{M-1})] \leq 0.$$

The rest of the proof is by induction. Suppose that  $U_{i+1} < U_{i+2} \leq U_M$  (the weak inequality is necessary to encompass the case where  $i = M - 2$ ). By contradiction, assume that  $U_i \geq U_{i+1}$ . From the value of unemployment, we know that  $U_i \geq U_{i+1}$  implies that  $W_{L,i} - U_i \geq W_{L,i+1} - U_{i+1}$ . Using the same strategy as above, we have

$$\begin{aligned} \omega_{L,i+1} - \omega_{L,i} &= \tau(\bar{f}_{i+1} - \bar{f}_i) + (1 - \tau)(1 - \beta)(U_{i+1} - U_i) \\ &\quad - (1 - \tau)\lambda\beta[\pi_{i+1}(U_M - U_{i+2}) + (U_{i+2} - U_{i+1}) - \pi_i(U_M - U_{i+1}) - (U_{i+1} - U_i)] \\ &= \tau(\bar{f}_{i+1} - \bar{f}_i) + (1 - \tau)(1 - \beta(1 - \lambda))(U_{i+1} - U_i) \\ &\quad - (1 - \tau)\lambda\beta[(\pi_{i+1} - \pi_i)U_M + (1 - \pi_{i+1})U_{i+2}] - (1 - \pi_i)U_{i+1}. \end{aligned}$$

Finally, the firms' value functions implies that

$$\begin{aligned}
& (1 - \beta(1 - \lambda)(1 - \delta))(J_{L,i+1} - J_{L,i}) \\
&= (\bar{f}_{i+1} - \bar{f}_i) - (\omega_{L,i+1} - \omega_{L,i}) + (\pi_{i+1} - \pi_i)\beta\lambda(1 - \delta)J_M \\
&= (1 - \tau)(\bar{f}_{i+1} - \bar{f}_i) - (1 - \tau)(1 - \beta(1 - \lambda))(U_{i+1} - U_i) \\
&\quad + (1 - \tau)\lambda\beta[(\pi_{i+1} - \pi_i)U_M + (1 - \pi_{i+1})U_{i+2} - (1 - \pi_i)U_{i+1}] \\
&\geq (1 - \tau)(\bar{f}_{i+1} - \bar{f}_i) - (1 - \tau)(1 - \beta(1 - \lambda))(U_{i+1} - U_i) \\
&\quad + (1 - \tau)\lambda\beta[(\pi_{i+1} - \pi_i)U_{i+2} + (1 - \pi_{i+1})U_{i+2} - (1 - \pi_i)U_{i+1}] \\
&= (1 - \tau)(\bar{f}_{i+1} - \bar{f}_i) - (1 - \tau)(1 - \beta(1 - \lambda))(U_{i+1} - U_i) \\
&\quad + (1 - \tau)\lambda\beta(1 - \pi_i)(U_{i+2} - U_{i+1}) \\
&\geq 0,
\end{aligned}$$

again violating Nash Bargaining. It follows that  $U_i < U_{i+1}$ ,  $i = 1, \dots, M - 1$ .

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