

Economics 326

Methods of Empirical Research in Economics

Lecture 21: Multiple linear IV model and two-stage  
least squares (2SLS)

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## Multiple linear IV model

- ▶ In empirical research, we often have to estimate models that include multiple endogenous and exogenous regressors.
- ▶ Example:

$$\ln Wage_i = \gamma_0 + \gamma_1 Age_i + \gamma_2 Sex_i + \beta_1 Educ_i + \beta_2 Children_i + U_i.$$

- ▶ **Exogenous** regressors: age, sex, and a constant.
- ▶ **Endogenous** regressors: education and children (family size).

## Multiple linear IV model

- ▶ Consider the following model:

$$y_i = \gamma_0 + \gamma_1 X_{1,i} + \dots + \gamma_k X_{k,i} + \beta_1 Y_{1,i} + \dots + \beta_m Y_{m,i} + U_i,$$

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- ▶  $Y_{1,i}, \dots, Y_{m,i}$  are the  $m$  **endogenous** regressors:

$$\text{Cov}(Y_{1,i}, U_i) \neq 0, \dots, \text{Cov}(Y_{k,i}, U_i) \neq 0.$$

# Identification problem

- ▶ There are  $k + 1 + m$  unknown coefficients

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- ▶ There are more unknowns than equations. Thus, the knowledge of the true covariances between  $X$ 's,  $Y$ 's and  $y$  is not sufficient to recover the unknown coefficients

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$$\gamma_0, \gamma_1, \dots, \gamma_k, \beta_1, \dots, \beta_m.$$

- ▶ Without additional information, the coefficients are **not identified** even at the population level.
- ▶ We need **at least**  $m$  additional equations!

# IVs

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- ▶ The **necessary** condition for identification is that the number of equations is at least as large as the number of unknowns or  $l \geq m$ .

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and  $m$  **first-stage (reduced-form)** equations:

$$Y_{1,i} = \pi_{0,1} + \pi_{1,1} Z_{1,i} + \dots + \pi_{l,1} Z_{l,i} + \pi_{l+1,1} X_{1,i} + \dots + \pi_{l+k,1} X_{k,i} + V_{1,i},$$

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- ▶ Note that in general the exogenous regressors  $X$ 's can be correlated with the endogenous regressors  $Y$ 's and therefore should be included in the first-stage equations.
- ▶ It is assumed that the exogenous regressors  $X$ 's and IVs  $Z$ 's are **uncorrelated** with the errors  $U$  and  $V$ 's.

## The order condition for identification

- ▶ The necessary condition for identification is that for every endogenous regressors  $Y$  we bring **at least** one exogenous variable  $Z$  **excluded from the structural equation**:

$$l \geq m.$$

- ▶ When  $l = m$ , the system is **exactly identified**.
- ▶ When  $l > m$ , the system is **overidentified**.
- ▶ When  $l < m$ , the system is underidentified, and the estimation of the **structural coefficients**  $\gamma$ 's and  $\beta$ 's is impossible.

## 2SLS estimation: the first stage

- ▶ Consider the first-stage equations:

$$\begin{aligned} Y_{1,i} &= \pi_{0,1} + \pi_{1,1}Z_{1,i} + \dots + \pi_{l,1}Z_{l,i} \\ &\quad + \pi_{l+1,1}X_{1,i} + \dots + \pi_{l+k,1}X_{k,i} + V_{1,i}, \\ &\quad \dots \end{aligned}$$

$$\begin{aligned} Y_{m,i} &= \pi_{0,m} + \pi_{1,m}Z_{1,i} + \dots + \pi_{l,m}Z_{l,i} \\ &\quad + \pi_{l+1,m}X_{1,i} + \dots + \pi_{l+k,m}X_{k,i} + V_{m,i}. \end{aligned}$$

- ▶ All right-hand side variables are exogenous.
- ▶ The first stage coefficients  $\pi$ 's can be estimated consistently by OLS by regressing  $Y$ 's against  $Z$ 's and  $X$ 's.

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- ▶ Let  $\hat{\pi}$ 's denote the OLS estimators of  $\pi$ .
- ▶ After estimating  $\pi$ 's, obtain the fitted (predicted) values for  $Y$ 's:

$$\begin{aligned}\hat{Y}_{1,i} &= \hat{\pi}_{0,1} + \hat{\pi}_{1,1}Z_{1,i} + \dots + \hat{\pi}_{l,1}Z_{l,i} \\ &\quad + \hat{\pi}_{l+1,1}X_{1,i} + \dots + \hat{\pi}_{l+k,1}X_{k,i}, \\ &\quad \dots \\ \hat{Y}_{m,i} &= \hat{\pi}_{0,m} + \hat{\pi}_{1,m}Z_{1,i} + \dots + \hat{\pi}_{l,m}Z_{l,i} \\ &\quad + \hat{\pi}_{l+1,m}X_{1,i} + \dots + \hat{\pi}_{l+k,m}X_{k,i}.\end{aligned}$$

- ▶  $\hat{Y}$ 's are functions of  $Z$ 's and  $X$ 's (all exogenous) and asymptotically uncorrelated with the errors.

## 2SLS: the second stage

- ▶ In the second stage, regress (OLS) the dependent variable  $y$  against a constant,  $X$ 's, and  $\hat{Y}$ 's obtained in the first stage:

$$y_i = \hat{\gamma}_0^{2SLS} + \hat{\gamma}_1^{2SLS} X_{1,i} + \dots + \hat{\gamma}_k^{2SLS} X_{k,i} + \hat{\beta}_1^{2SLS} \hat{Y}_{1,i} + \dots + \hat{\beta}_m^{2SLS} \hat{Y}_{m,i} + \hat{U}_i$$

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- ▶ One can show that the resulting 2SLS estimators  $\hat{\gamma}_0^{2SLS}, \hat{\gamma}_1^{2SLS}, \dots, \hat{\gamma}_k^{2SLS}, \hat{\beta}_1^{2SLS}, \dots, \hat{\beta}_m^{2SLS}$  are consistent and asymptotically normal.

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- ▶ When using the above steps to obtain the 2SLS estimates, the standard errors reported from the second-stage OLS estimation do not take into the account that  $\hat{Y}$ 's were constructed using  $\hat{\pi}$ 's and not the true (unknown)  $\pi$ 's. Therefore, they are incorrect and have to adjusted for the estimation error in the first stage.

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- ▶ Most statistical packages have pre-programmed procedures that report the estimation results for both stages and report the corrected standard errors for the second stage.

- ▶ In Stata, 2SLS estimator can be obtained using the command `ivregress 2sls`. The command accepts the options `robust` to compute heteroskedasticity robust standard errors and `first` to report the first stage.

```
. ivregress 2sls lwage (educ=motheduc fatheduc) exper expersq, robust first
```

#### First-stage regressions

```
Number of obs =      428
F( 4, 423) =      25.76
Prob > F      =      0.0000
R-squared     =      0.2115
Adj R-squared =      0.2040
Root MSE     =      2.0390
```

	educ	exper	expersq	motheduc	fatheduc	_cons
Coef.	.0452254	-.0010091	.157597	.1895484	9.10264	
Robust Std. Err.	.0419107	.0013233	.0354502	.0324419	.4241444	
t	1.08	-0.76	4.45	5.84	21.46	
P> t	0.281	0.446	0.000	0.000	0.000	
[95% Conf. Interval]	-.0371538 .1276046	-.0036101 .0015919	.0879165 .2272776	.125781 .2533159	8.268947 9.936333	

Instrumental variables (2SLS) regression

Number of obs = 428  
 Wald chi2(3) = 18.61  
 Prob > chi2 = 0.0003  
 R-squared = 0.1357  
 Root MSE = .67155

	Coef.	Robust Std. Err.	z	P> z	[95% Conf. Interval]	
lwage						
educ	.0613966	.0331824	1.85	0.064	-.0036397	.126433
exper	.0441704	.0154736	2.85	0.004	.0138428	.074498
expersq	-.000899	.0004281	-2.10	0.036	-.001738	-.00006
_cons	.0481003	.4277846	0.11	0.910	-.7903421	.8865427

Instrumented: educ

Instruments: exper expersq motheduc fatheduc

- For comparison, the OLS estimates are below:

. regress lwage educ exper expersq, robust

	Coef.	Robust Std. Err.	t	P> t	[95% Conf. Interval]	
lwage						
educ	.1074896	.013219	8.13	0.000	.0815068	.1334725
exper	.0415665	.015273	2.72	0.007	.0115462	.0715868
expersq	-.0008112	.0004201	-1.93	0.054	-.0016369	.0000145
_cons	-.5220406	.2016505	-2.59	0.010	-.9183996	-.1256815