Paul Schrimpf

Demand and supply of differentiated products

Paul Schrimpf

UBC Economics 567

January 23, 2024

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic space

Early work

Model

Model

identification

Aggregate product data

Estimation steps

Pricing equati

Micro data

References

References

1 Introduction

2 Demand in product space

Demand in characteristic space
Early work
Model
Estimation and identification
Aggregate product data
Estimation steps
Pricing equation
Micro data



References

differentiated products Paul Schrimpf

Demand and supply of

Introduction

Demand in product space

- Demand in characteristic space
- Early wor
- Model
- Model
- Estimation and identification
- Aggregate product data
- Estimation steps
- Pricing equation

References

References

• Reviews:

- Gandhi and Nevo (2021)
- Berry and Haile (2021)
- Aguirregabiria (2021) chapter 2
- Hortaçsu and Joo (2023) 2.1-2.2 and chapter 3
- Ackerberg et al. (2007) section 1 (these slides use their notation)
- Reiss and Wolak (2007) sections 1-7, especially 7
- Classic papers:
 - Berry (1994)
 - Berry, Levinsohn, and Pakes (1995)

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic space Farly work

Model

Model

Estimation and identification

Aggregate product data

Estimation steps

Pricing equatio

Micro data

References

References

Section 1

Introduction

Introduction

products Paul Schrimpf

Demand and supply of

differentiated

Introduction

- Demand in characteristic space
- Early worl
- Model
- Model
- Estimation and identification
- Aggregate product data
- Estimation steps
- Pricing equation
- References
- References

- Typical market for consumer goods has many differentiated, but similar products, e.g.
 - Cars
 - Cereal
- Differentiated products are a source of market power
- Having many products can result in many parameters creating estimation difficulties and requiring departures from textbook demand and supply models

Motivation

products Paul Schrimpf

Demand and supply of

differentiated

Introduction

- Demand in characteristic space
- Early wor
- Model
- Model
- Estimation and identification
- Aggregate product data
- Estimation steps
- Pricing equatio
- References
- References

- Counterfactuals that do not change production technology
 - Mergers
 - Tax changes
- Effects of new goods
- Cost-of-living indices
- Product differentiation and market power
 - Cross-price elasticities

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic space

Early work

Model

Estimation ar

identification Aggregate product

data

Estimation step:

Micro data

Millio data

References

References

Section 2

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic space Early work Model Model

Estimation and identification

Aggregate product data

Estimation steps

Pricing equatio

Initio uata

References

References

Demand in product space 1

J products, each treated as separate good Classical demand,

$$\begin{split} & q_1 = D_1(p_1, ..., p_J, z_1, \eta_1; \beta_1) \\ & \vdots = \vdots \\ & q_J = D_J(p_1, ..., p_J, z_J, \eta_J; \beta_J), \end{split}$$

and supply (firms' first-order conditions for prices):

$$p_{1} = g_{1}(q_{1}, ..., q_{J}, w_{1}, v_{1}; \theta_{1})$$

$$\vdots = \vdots$$

$$p_{J}^{d} = g_{J}(q_{1}, ..., q_{J}, w_{J}, v_{J}; \theta_{J}),$$

where

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic

space

Early wor

Model

Model

identification

Aggregate product data

Estimation step:

Pricing equation

References

References

- $p_j = price$
- $q_j = quantity$
- z_j = observed demand shifter
- η_j = unobserved demand shock
- β_j = demand parameters
- w_j = observed supply shifter
- v_j = unobserved supply shock
- $\theta_j = \text{supply parameters}$
- *D_j* typically parametrically specified, e.g.

$$\ln q_j = \beta_{j0} + \beta_{j1}p_1 + \cdots + \beta_{jJ}p_J + \beta_{jy}\ln y + Z_1\gamma + \nu_j$$

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic space ^{Early work} Model

Model

Estimation and identification

Aggregate product data

Estimation steps

Pricing equation

Deferences

References

Demand in product space

• Use reduced form to find instruments

 $q_{1} = \Pi_{1}^{q}(Z, W, v, \eta; \beta, \theta)$ $\vdots = \vdots$ $q_{J} = \Pi_{J}^{q}(Z, W, v, \eta; \beta, \theta)$ $p_{1} = \Pi_{1}^{p}(Z, W, v, \eta; \beta, \theta)$ $\vdots = \vdots$ $p_{I} = \Pi_{I}^{p}(Z, W, v, \eta; \beta, \theta)$

- Cost shifters of product *j* excluded from demand and supply of product *k*, but in reduced form
 - Cost data often not available
 - If available, unlikely to be product specific
- Attributes of other products
 - Hausman (1996) uses prices of other products
 - Hard to justify, especially with prices

Paul Schrimpf

Introduction

Demand in product space

- Demand in characteristic space
- Early worl
- Model
- Model
- Estimation and identification
- Aggregate product data
- Estimation steps
- Pricing equation
- References
- References

- Advantages of product space:
 - Flexible substitution patterns
 - Does not require detailed product attribute data
- Problems with product space:
 - 1 Representative agent and aggregation issues
 - With heterogeneous preferences, aggregate market demand need not meet restrictions on individual demand derived from economic theory
 - Cannot use restrictions easily to improve estimates
 - Can use simulation to aggregate (Pakes, 1986)
 - **2** Too many parameters, $O(J^2)$
 - Can limit by restricting cross-price elasticities, e.g. Pinkse, Slade, and Brett (2002)
 - 3 Too many instruments needed, J
 - 4 Cannot analyze new goods

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic space

Early worl

Model

Model

identification

Aggregate product data

Estimation steps

Pricing equatio

Micro data

References

References

Section 3

Demand in characteristic space

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic space

Early work

Model

Mode

Estimation and identification

Aggregate product data

Estimation steps

Pricing equatio

Micro data

References

References

Demand in characteristic space

• Why do firms differentiate products?

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic space

- Early work
- Model
- Model
- Estimation and identification
- Aggregate product data
- Estimation steps
- Pricing equation
- Micro data
- References
- References

Demand in characteristic space

- Why do firms differentiate products?
- Because consumers have heterogeneous tastes for product characteristics
 - E.g. cars: tastes for size, safety, fuel efficiency, etc

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic space

Early work

Model

Model

Estimation and identification

Aggregate product data

Estimation steps

Pricing equatio

Micro data

References

References

Demand in characteristic space

• Model consumer preferences for characteristics and treat products as bundles of characteristics

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic space

- Early wor
- Model
- Model
- Estimation and identification
- Aggregate product data
- Estimation steps
- Pricing equatio
- Micro data
- References
- References

Demand in characteristic space

- Model consumer preferences for characteristics and treat products as bundles of characteristics
- Reduces number of parameters
- Predict demand for new goods
- Demand system consistent with utility maximization

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic space

Early worl

Model

Model

Estimation and identification

Aggregate product data

Estimation steps

Pricing equation

References

References

Demand in characteristic space

- Model consumer preferences for characteristics and treat products as bundles of characteristics
- Reduces number of parameters
- Predict demand for new goods
- Demand system consistent with utility maximization
- Early work: Lancaster (1971), McFadden (1973)
- Key extension to early work: Berry, Levinsohn, and Pakes (1995)

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic space

Early work

Model

Estimation and identification

Aggregate product data

Estimation steps

Pricing equati

References

References

Early work in characteristic space

- Consumer chooses one or none of *J* products
- Utility of consumer *i* from product *j*

$$u_{ij} = x_j\beta + \epsilon_{ij}$$

with ϵ_{ij} iid across *i* and *j* (usually Type I extreme value)

• Implies aggregate demand (for Type I extreme value)

$$q_j = \frac{\exp(x_j\beta)}{1 + \sum_{k=1}^J \exp(x_k\beta)}$$

- Problem: restrictive substitution "independence of irrelevant alternatives"
 - Two goods with the same shares have the same cross price elasticities with any third good (think about a luxury and bargain good with equal shares)
 - Goods with same shares should have same markups
- Solution: add heterogeneity in β and/or allow correlation across *j* in ϵ_{ij}

Model 1

products Paul Schrimpf

Demand and supply of

differentiated

Introduction

- Demand in product space
- Demand in characteristic space
- Early work
- Model
- Model
- Estimation and identification
- Aggregate product data
- Estimation steps
- Pricing equatio
- Micro data
- References
- References

- Consumers *i*, goods *j*, markets *t*
- Utility: (include good 0 = buy nothing)



- $x_{jt} = (\tilde{x}_{jt}, p_{jt}) \in \mathbb{R}^{K}, z_{it} \in \mathbb{R}^{R}, v_{it} \in \mathbb{R}^{L}$
- Choose *j* if $u_{ijt} > u_{ikt} \ \forall k \neq j$

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic space

- Early work
- Model

Model

Estimation and identification

- Aggregate product data
- Estimation steps
- Pricing equati

References

References

• Usually U(·) linear:



Model 1

- for j = 1...J and normalize $u_{i0t} = 0$
- Assume ϵ_{ijt} i.i.d. double exponential
- Assume $v_{it} \sim f_v(\cdot; \theta)$, e.g. independent normal
- Write as product specific + observed interactions + unobserved interactions

$$u_{ijt} = \underbrace{\delta_j}_{=x_{jt}\bar{\theta} + \xi_{jt}} + x_{jt}\underbrace{\theta^o}_{K \times R} Z_{it} + x_{jt}\underbrace{\theta^u}_{K \times L} v_{it} + \epsilon_{ijt}$$

Endogeneity

products Paul Schrimpf

Demand and supply of

differentiated

Introduction

Demand in product space

Demand in characteristic space

Early work

Model

Model

Estimation and identification

Aggregate product data

Estimation steps

Pricing equation

.....

References

References

• Usually assume $E[v_{it}|x_{jt}, z_{it}] = 0$ and $E[\epsilon_{ijt}|x_{jt}, z_{it}] = 0$

• Not interested in counterfactuals with respect to changes in *z_{it}*, so can treat as residual, i.e.

$$v_{it} = \theta_{it} - \mathsf{E}[\theta_{it}|\mathbf{z}_{it}]$$

• Market average v_{it} or ϵ_{ijt} plausibly correlated with p_{jt} or other product characteristics, but this correlation absorbed into ξ_{jt} and/or market fixed effects

Endogeneity

products Paul Schrimpf

Demand and supply of

differentiated

Introduction

Demand in product space

Demand in characteristic space

- Early work
- Model

Model

- Estimation and identification
- Aggregate product data
- Estimation steps
- Pricing equatio
- Micro data
- References
- References

- Problem is ξ_{jt}
 - Prices and other flexible product characteristics must be correlated with ξ_{jt}
 - If ξ_{jt} serially correlated, then likely also correlated with inflexible product characteristics
 - Need instrument, w_{jt} such that $E[\xi_{jt}|w_{jt}] = 0$
 - Cost shifters
 - Characteristics of other products

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic space

Early work

Model

Model

Estimation and identification

Aggregate product data

Estimation steps

Pricing equation

Micro data

References

References

Estimation and identification

- Depends on data:
 - Aggregate product market shares and characteristics
 - Individual characteristics and choices
- Additional assumptions:
 - Use supply and equilibrium assumptions to get a pricing equation

Paul Schrimpf

Introduction

Demand in product space

- Demand in characteristic space
- Early work
- Model
- Model

Estimation and identification

Aggregate product data

Estimation step

Pricing equatio

Micro data

References

References

Aggregate data 1

- Often only have data on product characteristics and market shares
- Maybe also distribution of some individual characteristics for each market (e.g. income and education from CPS or census)
- Instrument *w* such that $E[\xi_j|w] = 0$
- Distribution of $v \sim f_v(\cdot; \theta_v)$
 - Combination of estimated market level distribution of observed individual characteristics and parametric distributions of unobserved individual characteristics

$$F_{\nu,t}(s, y, e; \theta_{\nu}) = \underbrace{\hat{F}_t(s, y)}_{\text{empirical distribution}} \Phi\left(\frac{e - \theta_{\nu}^{\mu}}{\theta_{\nu}^{\sigma}}\right)$$

 $\hat{F}_t(s, y)$ estimated from CPS or other similar data set

Aggregate data 2

Paul Schrimpf

Demand in product space

- Demand in characteristic space
- Early work
- Model
- Model
- Estimation and identification

Aggregate product data

- Estimation steps
- Pricing equation
- Micro data
- References
- References

- Assume $\epsilon_{ijt} \sim$ double exponential (aka Gumbel or type I extreme value) as in logit
 - Computationally convenient, but other distributions feasible too

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic space

Early worl

Model

Model

Estimation and identification

Aggregate product data

Estimation steps

Pricing equatio

References

References

Estimation outline

• Estimate θ from moment condition

 $\mathsf{E}[\xi(\cdot;\theta)|w] = \mathbf{0}$

- Where ξ(·; θ) is such that model predicted market shares = observed market shares¹
 - **1** Compute shares given θ , $\sigma(\cdot; \theta, \delta)$
 - 2 Find $\delta(\cdot; \theta) = x_{jt}\bar{\theta} + \xi(\cdot; \theta)$ such that observed shares, s_{jt} = model shares, $\sigma(\cdot; \theta, \delta)$, then

$$\xi(\cdot;\theta) = \delta(\cdot;\theta) - x_{jt}\bar{\theta}$$

¹In this slide \cdot means the data. I will leave the \cdot out of the notation in subsequent slides. I will also leave out *t* subscripts.

Paul Schrimpf

Introduction

Demand in product space

- Demand in characteristic space
- Early work
- Model
- Model

Estimation and identification

Aggregate product data

Estimation steps

Pricing equation

References

References

Computing model shares

• Integrate over v

$$\sigma_{j}(\theta, \delta) = \int \frac{\exp(\delta_{j} + x_{j}\theta^{u}v)}{1 + \sum_{k=1}^{j}\exp(\delta_{k} + x_{k}\theta^{u}v)} dF_{v}(v)$$

• Integral typically has no closed form, so compute numerically, usually by Monte Carlo integration

$$\sigma_j(\theta, \delta) = \sum_{r=1}^{N_s} \frac{\exp(\delta_j + x_j \theta^u v_r)}{1 + \sum_{k=1}^j \exp(\delta_k + x_k \theta^u v_r)}$$

where v_r are N_s random draws from f_v

- Issues about how best to compute integral simulation vs quadrature, type of simulation (Skrainka and Judd, 2011)
- Simulation (more generally approximation) of integral affects distribution of estimator

Paul Schrimpf

Introduction

Demand in product space

- Demand in characteristic space
- Early work
- Model
- Model
- Estimation and identification
- Aggregate product data

Estimation steps

Pricing equation Micro data

References

References

Solving for δ and ξ

- Want δ s.t. $\sigma_j(\theta, \delta) = \hat{s}_j$
- Berry, Levinsohn, and Pakes (1995) show

$$T(\delta) = \delta + \log(\hat{s}_j) - \log(\sigma_j(\theta, \delta))$$

is a contraction

- Unique fixed point δ such that $\delta = \delta + \log(\hat{s}_i) - \log(\sigma_i(\theta, \delta))$, i.e. $\hat{s}_i = \sigma_i(\theta, \delta)$
- Can compute $\delta(\theta)$ by repeatedly applying contraction (in theory and practice often faster to use other method)
- $\xi_j(\theta) = \delta_j(\theta) x_j \bar{\theta}$
- Important identifying assumption: only θ s.t. $\xi_j(\theta) = \xi_j^0$ is true θ_0

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic

Farly wor

Model

Model

Estimation and identification

Aggregate product data

Estimation steps

Pricing equation Micro data

References

References

Conditional moment restriction E[ξ_j(θ)|w] = 0
Empirical unconditional moments:

$$G_{J,T,N,N_s} = \frac{1}{JT} \sum_{j=1}^J \sum_{t=1}^T \xi_{jt}(\theta) f(w_t)$$

where

- f(w) = vector of function of w
- *J* = number of products
- *T* = number of markets
- N = number of observations in each market underlying \hat{s}_i
- $\dot{N}_{\rm s}$ = number of simulations
- Asymptotic properties (consistency, distribution), depend on which of J, T, N, and N_s are $\rightarrow \infty$, see Berry, Linton, and Pakes (2004)
- Reynaert and Verboven (2014): using optimal instruments greatly improves efficiency and stability

Estimating θ

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic space

Early worl

Model

Model

Estimation and identification

Aggregate product data

Estimation steps

Pricing equation

References

References

Pricing equation 1

- More moments give more precise estimates
- Assumption about form of equilibrium allows use of firm first order condition (pricing equation) as additional moment
- Nash equilibrium in prices
- Log linear marginal cost

$$\log mc_j = r_j \theta^k + \omega_j$$

- r_j = observed product characteristics, input prices, maybe quantity, etc
- ω_j = unobserved productivity, possibly endogenous
- Firm f producing set of product \mathcal{J}_f ,

$$\max_{p_j: j \in \mathcal{J}_f} \sum_{j \in \mathcal{J}_f} (p_j - C_j(\cdot)) Ms_j(\cdot, p)$$

Paul Schrimpf

Introduction

Demand in product space

- Demand in characteristic space
- Early work
- Model
- Model
- Estimation and identification
- Aggregate product data
- Estimation steps

Pricing equation

Micro data

References

References

Pricing equation 2

• First order condition:

$$\sigma_j(\cdot) + \sum_{l \in \mathcal{J}_f} (p_l - mc_l) \frac{\partial \sigma_l(\cdot)}{\partial p_j} = 0$$

Collect as

$$s + (p - mc)\Delta = 0$$

Rearrange and use log linear marginal cost

$$\log(\boldsymbol{p} - \Delta^{-1}\sigma) - \boldsymbol{r}\theta^{\mathsf{c}} = \omega(\theta)$$

- Conditional moment restriction $E[\omega(\theta)|w] = 0$
- Add empirical moments to G, $\frac{1}{JT} \sum_{jt} \omega_{jt}(\theta) f(w_t)$

Paul Schrimpf

Introduction

Demand in product space

- Demand in characteristic space
- Early work
- Model
- Model
- Estimation and identification
- Aggregate product data
- Estimation steps
- Pricing equation

Micro data

References

References

• Berry, Levinsohn, and Pakes (2004)

Data on individual choices and characteristics

$$u_{ijt} = \underbrace{\delta_j}_{=x_{jt}\bar{\theta} + \xi_{jt}} + x_{jt}\underbrace{\theta^o}_{K \times R} Z_{it} + x_{jt}\underbrace{\theta^u}_{K \times L} v_{it} + \epsilon_{ijt}$$

- Random coefficients discrete choice model, so can identify and estimate δ, θ^o, and θ^u without assumptions about ξ and x
 - Ichimura and Thompson (1998) give conditions for nonparametric identification of random coefficients binary choice models
 - Estimate by MLE or (usually) GMM
- Still need $\bar{\theta}$ for price elasticities, etc

$$\delta_j = x_{jt}\bar{\theta} + \xi_{jt}$$

- Use IV
- Use IV with a pricing equation

Micro data

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic space

Early work

Model

Estimation and identification

Aggregate product data

Estimation steps

Pricing equation

Micro data

References

References

Section 4

References

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic space

- Early work
- Model
- Model

Estimation and identification

Aggregate product data

Estimation steps

Pricing equation

References

References

Ackerberg, D., C. Lanier Benkard, S. Berry, and A. Pakes. 2007. "Econometric tools for analyzing market outcomes." Handbook of econometrics 6:4171-4276. URL http://www.sciencedirect.com/science/article/ pii/S1573441207060631. Ungated URL http://people.stern.nyu.edu/acollard/Tools.pdf. Aguirregabiria, Victor. 2021. "Empirical Industrial Organization: Models, Methods, and Applications." URL

http:

//aguirregabiria.net/wpapers/book_dynamic_io.pdf.

Berry, S., J. Levinsohn, and A. Pakes. 2004. "Differentiated Products Demand Systems from a Combination of Micro and Macro Data: The New Car Market." *Journal of Political Economy* 112 (1):68–105. URL http://www.jstor.org/stable/10.1086/379939.

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic space Early work

Model

Estimation and identification

Aggregate product data

Estimation steps

Pricing equation

MICro data

References

References

Berry, Steve, Oliver B. Linton, and Ariel Pakes. 2004. "Limit Theorems for Estimating the Parameters of Differentiated Product Demand Systems." The Review of Economic Studies 71 (3):613-654. URL http://restud.oxfordjournals. org/content/71/3/613.abstract.

Berry, Steven, James Levinsohn, and Ariel Pakes. 1995."Automobile Prices in Market Equilibrium." *Econometrica* 63 (4):pp. 841–890. URL

http://www.jstor.org/stable/2171802.

Berry, Steven T. 1994. "Estimating Discrete-Choice Models of Product Differentiation." *The RAND Journal of Economics* 25 (2):pp. 242–262. URL http://www.jstor.org/stable/2555829.

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic space Early work

Model

Estimation and identification

Aggregate product data

Estimation steps

Pricing equation

References

References

Berry, Steven T. and Philip A. Haile. 2021. "Chapter 1 -Foundations of demand estimation." In *Handbook of Industrial Organization, Volume 4, Handbook of Industrial Organization,* vol. 4, edited by Kate Ho, Ali Hortaçsu, and Alessandro Lizzeri. Elsevier, 1–62. URL

https://www.sciencedirect.com/science/article/ pii/S1573448X21000017.

Gandhi, Amit and Aviv Nevo. 2021. "Chapter 2 - Empirical models of demand and supply in differentiated products industries." In *Handbook of Industrial Organization, Volume 4, Handbook of Industrial Organization,* vol. 4, edited by Kate Ho, Ali Hortaçsu, and Alessandro Lizzeri. Elsevier, 63–139. URL https://www.sciencedirect.com/ science/article/pii/S1573448X21000029.

Hausman, J.A. 1996. "Valuation of new goods under perfect and imperfect competition." In *The economics of new goods*. University of Chicago Press, 207–248. URL http://www.nber.org/chapters/c6068.pdf.

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic space

Early worl

Model

Mode

Estimation and identification

Aggregate product data

Estimation steps

Pricing equation

References

References

Hortaçsu, Ali and Joonhwi Joo. 2023. Structural Econometric Modeling in Industrial Organization and Quantitative Marketing: Theory and Applications. Princeton University Press.

Ichimura, Hidehiko and T.Scott Thompson. 1998. "Maximum likelihood estimation of a binary choice model with random coefficients of unknown distribution." Journal of Econometrics 86 (2):269 - 295. URL http://www.sciencedirect.com/science/article/

pii/S0304407697001176.

Lancaster, K. 1971. *Consumer demand: A new approach.* Columbia University Press (New York).

McFadden, D. 1973. "Conditional logit analysis of qualitative choice behavior." Frontiers in Econometrics :105-142URL http://elsa.berkeley.edu/pub/reprints/mcfadden/ zarembka.pdf.

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic space

Model

Estimation and identification

Aggregate product data

Estimation steps

Pricing equati

References

References

Pakes, Ariel. 1986. "Patents as Options: Some Estimates of the Value of Holding European Patent Stocks." *Econometrica* 54 (4):pp. 755–784. URL http://www.jstor.org/stable/1912835.

Pinkse, J., M.E. Slade, and C. Brett. 2002. "Spatial price competition: a semiparametric approach." *Econometrica* 70 (3):1111-1153. URL http://onlinelibrary.wiley.com/ doi/10.1111/1468-0262.00320/abstract.

Reiss, P.C. and F.A. Wolak. 2007. "Structural econometric modeling: Rationales and examples from industrial organization." *Handbook of econometrics* 6:4277-4415. URL http://www.sciencedirect.com.ezproxy.library. ubc.ca/science/article/pii/S1573441207060643.

Reynaert, Mathias and Frank Verboven. 2014. "Improving the performance of random coefficients demand models: The role of optimal instruments." *Journal of Econometrics* 179 (1):83 – 98. URL http://www.sciencedirect.com/ science/article/pii/S0304407613002649.

Paul Schrimpf

Introduction

Demand in product space

Demand in characteristic space

Early wor

Model

Fotimotio

identification

Aggregate product data

Estimation steps

Pricing equatio

Micro data

References

References

Skrainka, B. and K. Judd. 2011. "High performance quadrature rules: How numerical integration affects a popular model of product differentiation." Available at SSRN 1870703. URL http://papers.ssrn.com/sol3/ papers.cfm?abstract_id=1870703.